

## Probabilistic Assessment of the Robustness of Structural Systems

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## Introduction

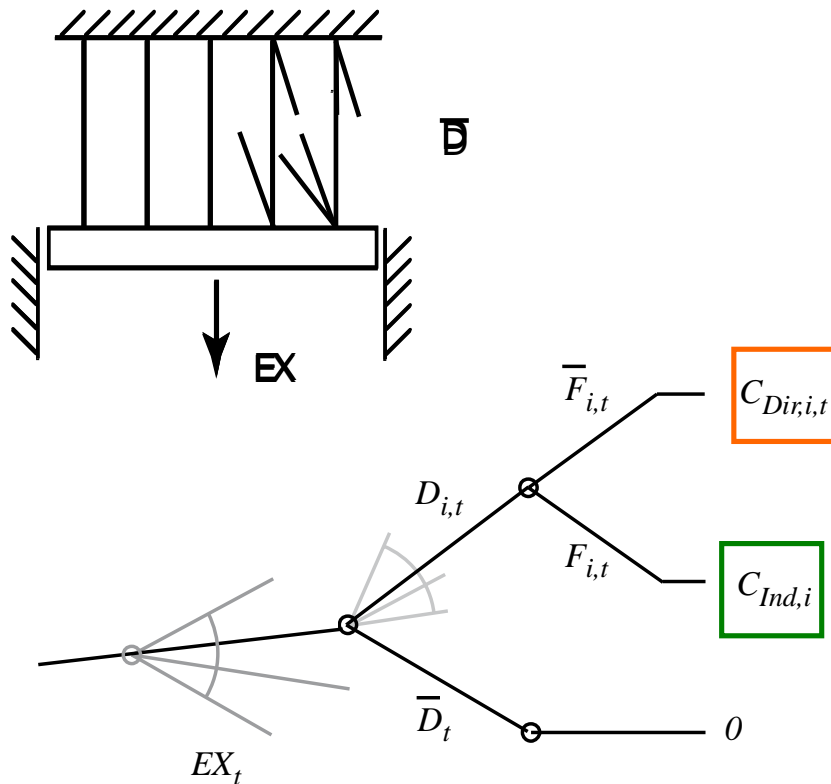
- Robustness is generally accepted as a characteristic of a good system design
- Objective quantification of robustness is needed
- A risk-based method for measuring robustness is proposed here
- Robustness is interpreted here as damage tolerance:  
“the consequences of structural failure should not be disproportional to the effect causing the failure”

## Introduction

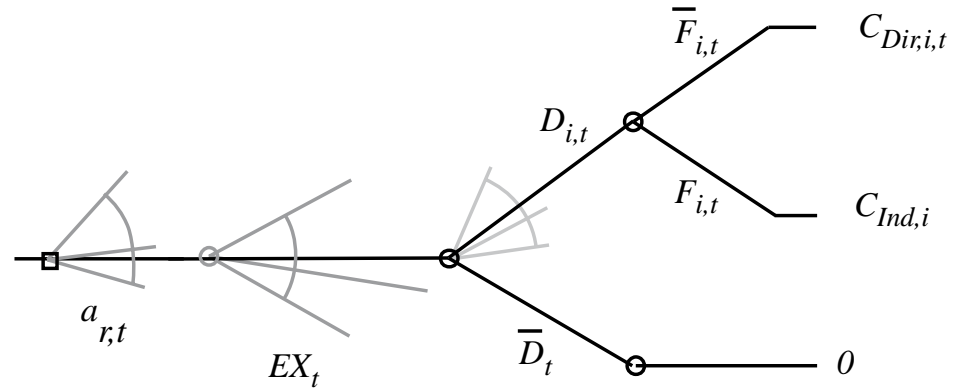
Desirable properties for a measure of robustness:

- General applicable to systems
- Allows for ranking of alternative systems
- Provides a criterion for identifying acceptable robustness

## Framework



$$I_{Rob} = \frac{\text{Direct Risk}}{\text{Direct Risk} + \text{Indirect Risk}}$$



Robustness is related to:

- Redundancy
- Ductility
- Reliability
- Behavior after damage
- Consequences

## The Index of Robustness

- Dependent upon the **probability of damage** occurrence
- Dependent upon **consequences**
- Depend upon the **exposure**
- Dependent upon **post damage actions**
- Is more than a characteristic of the structure

## Effect of deterioration on the robustness

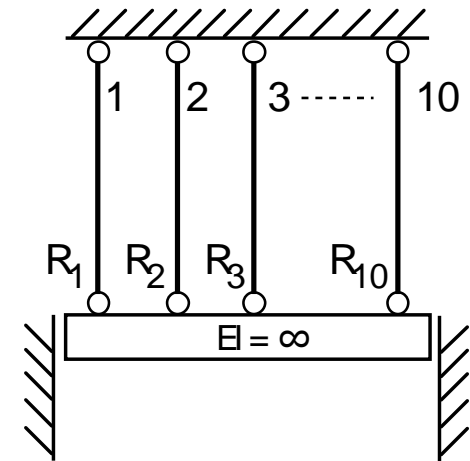
- Endogenous or exogenous effects might reduce the resistance over time
- The probability of failure and the probability of damage changes in time
- Intuitively, the robustness decreases over time



## Effect of deterioration on the robustness

### Structural System

- Parallel system with ten members
- Structural components are perfectly ductile
- Uniform redistribution of the load
- Marginal component failure probability  $10^{-3}$
- Initial resistance  $\sim \text{LN}(1.715, \text{CoV}=0.07)$
- Time dependent degradation function (Faber and Melchers, 2001)



$$R(t) = R_0 \cdot \psi(t_a)$$

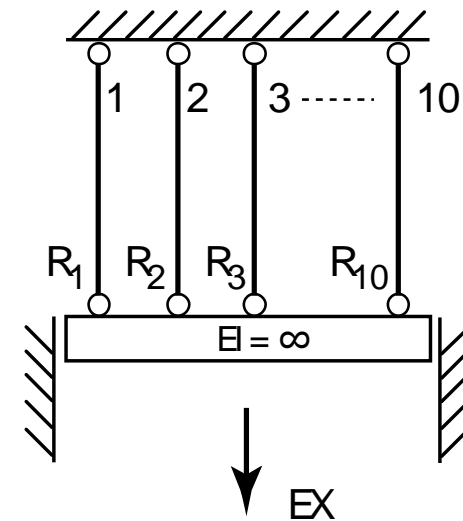
## Effect of deterioration on the robustness

### Exposure

- Dead load  $\sim N(0.3, \text{Cov}=0.1)$
- Live load  $\sim W(0.7, \text{Cov}=0.3)$

### Consequences

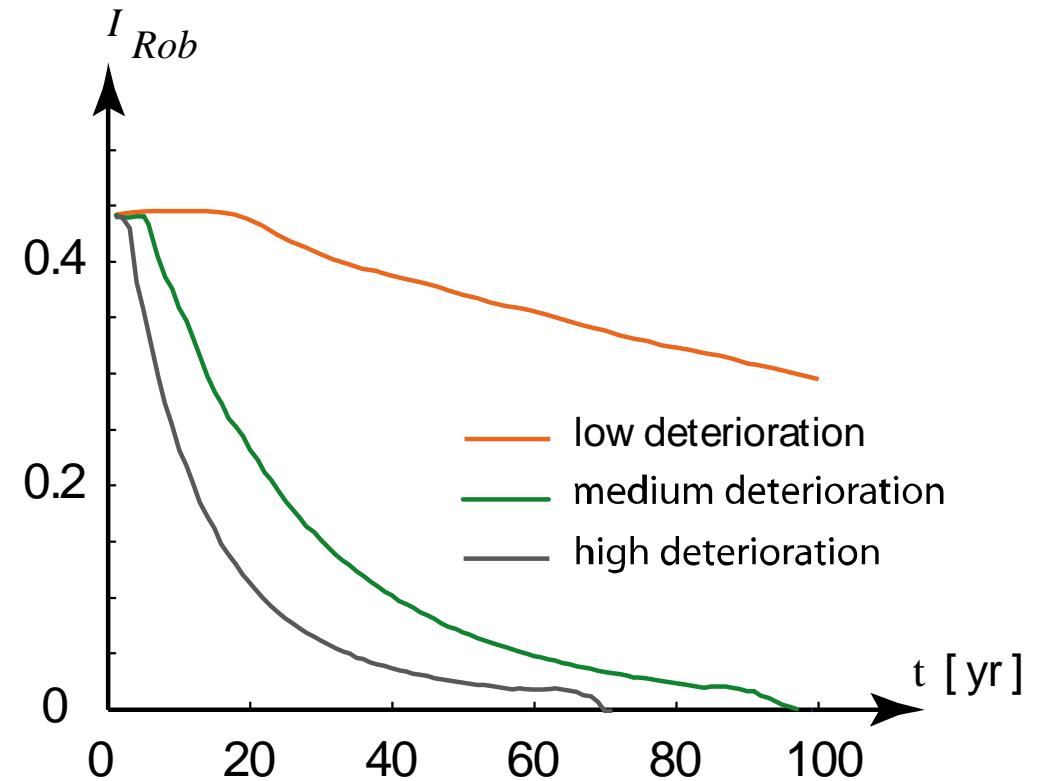
- Damage consequences for a single component is equal to one
- Failure consequences are 100 times the damage consequences





## Effect of deterioration on the robustness

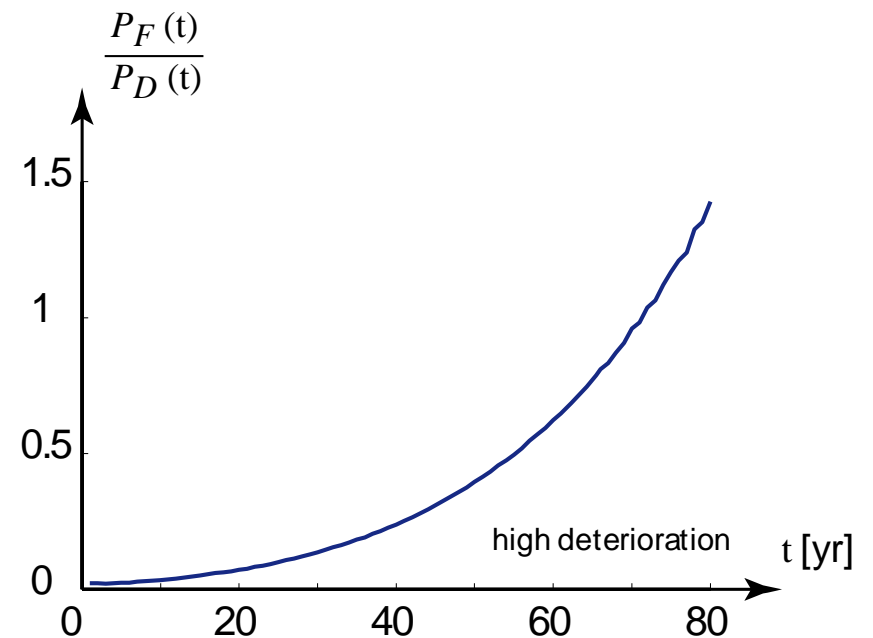
- Initial system is highly redundant
- The system seems to be robust
- The robustness decreases rapidly over time
- High robustness of the initial system compared to deteriorated system



## Effect of deterioration on the robustness

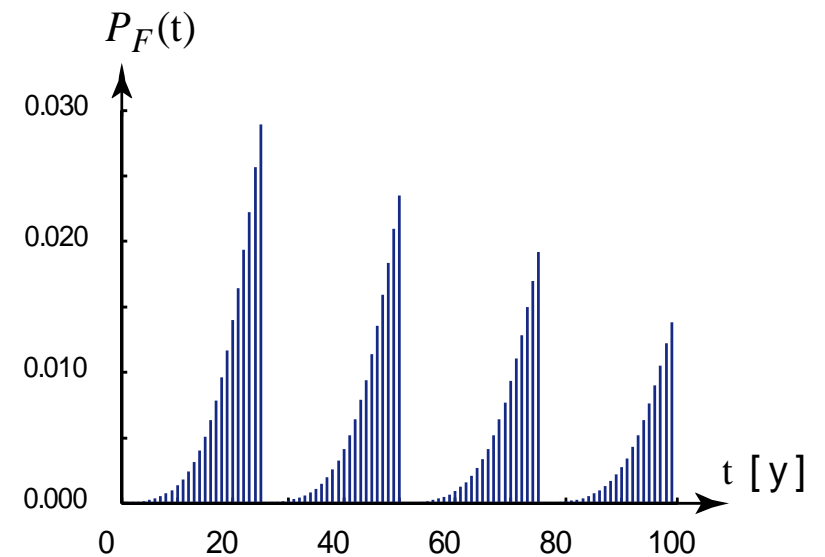
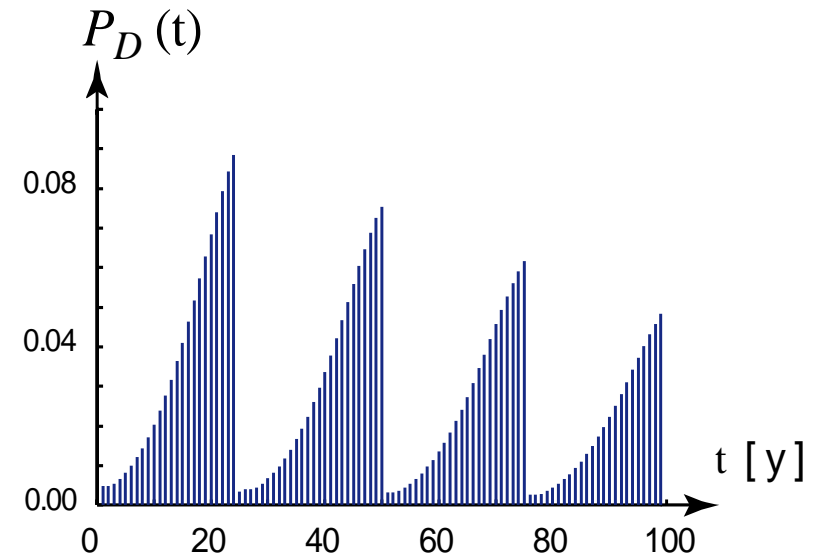
$$I_{Rob}(t) = \frac{\sum_i P_{D,i}(t) \cdot C_{Dir}}{\sum_i P_{D,i}(t) \cdot C_{Dir} + P_F(t) \cdot C_{Ind}} \approx \frac{P_{D,1}(t) \cdot C_{Dir}}{P_{D,1}(t) \cdot C_{Dir} + P_F(t) \cdot C_{Ind}} = \frac{C_{Dir}}{C_{Dir} + \frac{P_F(t)}{P_{D,1}(t)} \cdot C_{Ind}}$$

- Deterioration leads to a disproportional increase of the failure probability



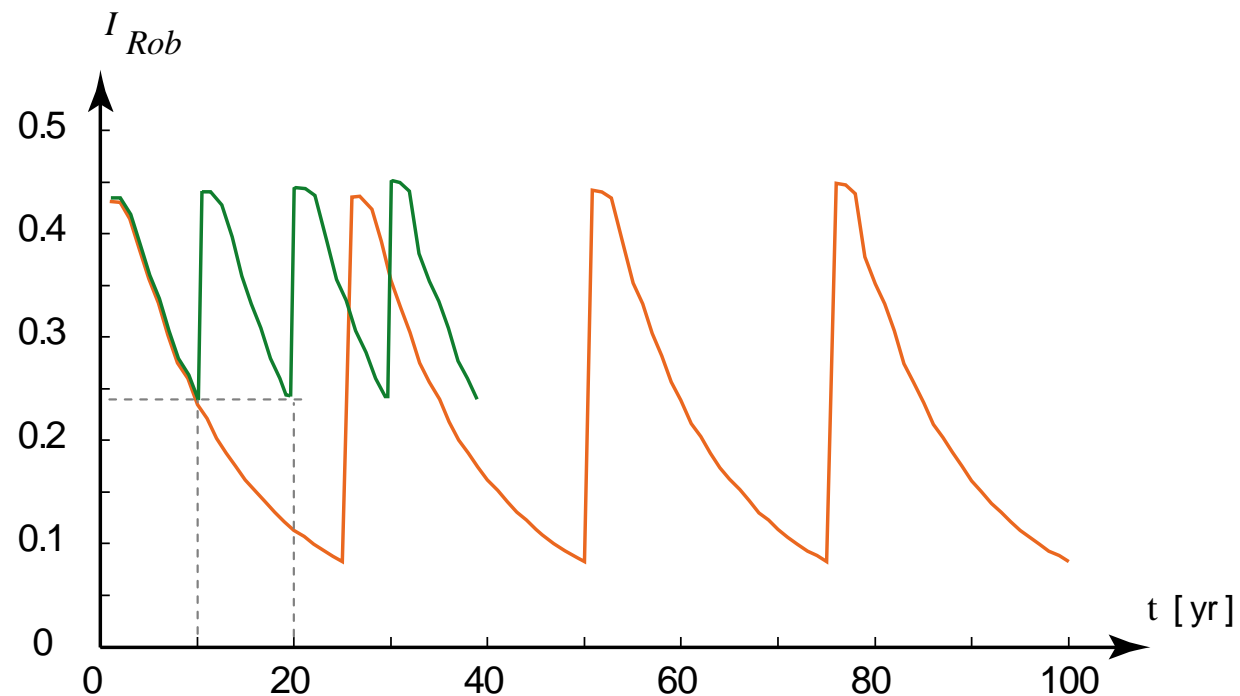
## Effect of inspections and repair actions

- High deterioration is assumed
- Inspection every 25 years
- Perfect repair actions are assumed



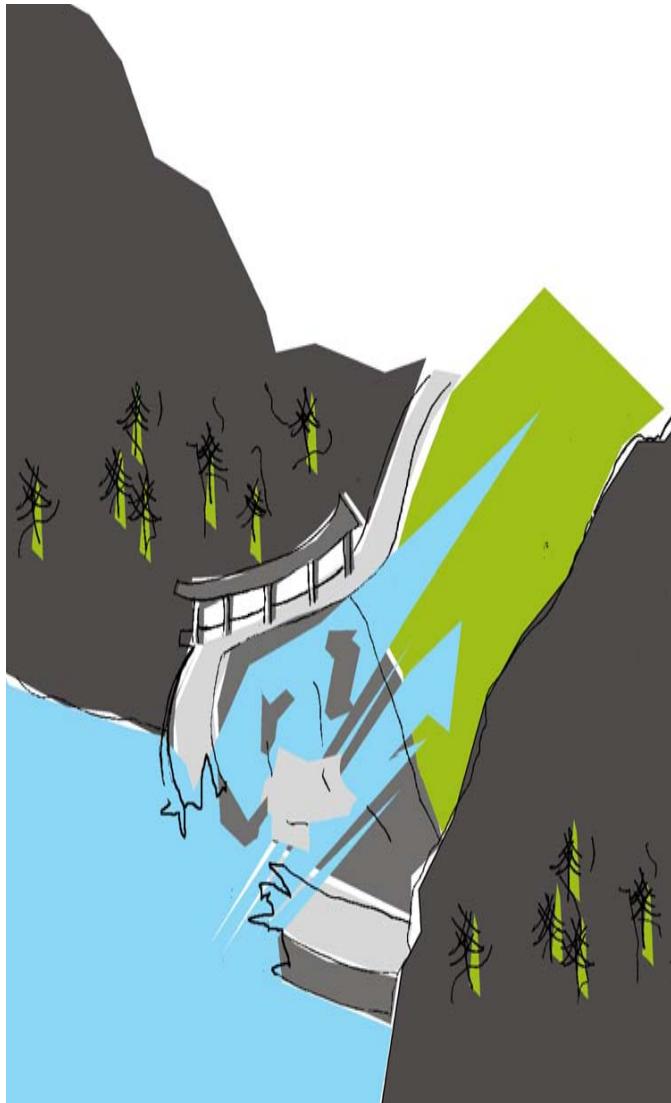
## Effect of inspections and repair actions

- Repair and maintenance actions can increase the robustness
- The robustness can be kept above a certain level
- Robustness calculations can help to identify repair and maintenance strategies.



## Conclusions

- The framework is based on risk assessment and decision theory
- The index of robustness facilitates the quantification of robustness
- It allows for the implementation of different mitigation measures over the life time of structural systems
- By implementing inspection and repair actions the robustness of a system can be controlled
- Further research is necessary to develop factors for a code based design including direct and indirect consequences.



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Thank you for your attention