

# **Risk and Safety**

**in**

# **Civil, Surveying and Environmental**

# **Engineering**

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# Contents of Today's Lecture

- Introduction to Bayesian Probabilistic Nets (BPN's)
- Causality as a support in reasoning
- Basic theory of BPN's with discrete states
- Risk analysis and decision making using BPN's
- Large Scale risk management using GIS and BPN's

# Introduction to Bayesian Probabilistic Nets (BPN's)

As stated many times previously

Risk analysis serves the purpose of decision making subject to uncertainty

Bayesian Probabilistic Networks (BPN) or Bayesian Belief Networks (BBN)

- were developed during the last decade for purposes of decision making in artificial intelligence engineering

Difficult problem  
many variables  
large uncertainties

Rule Based Systems

What would the "expert" do when and if ?

Not possible to treat uncertainties consistently !

Bad decisions – "Dutch Books"

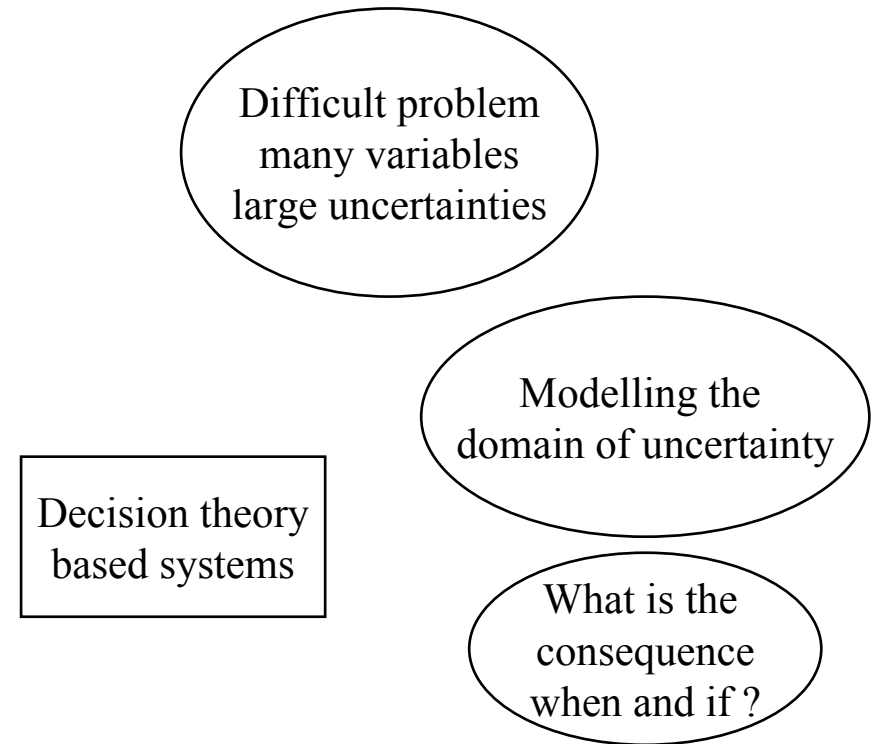
# Introduction to Bayesian Probabilistic Nets (BPN's)

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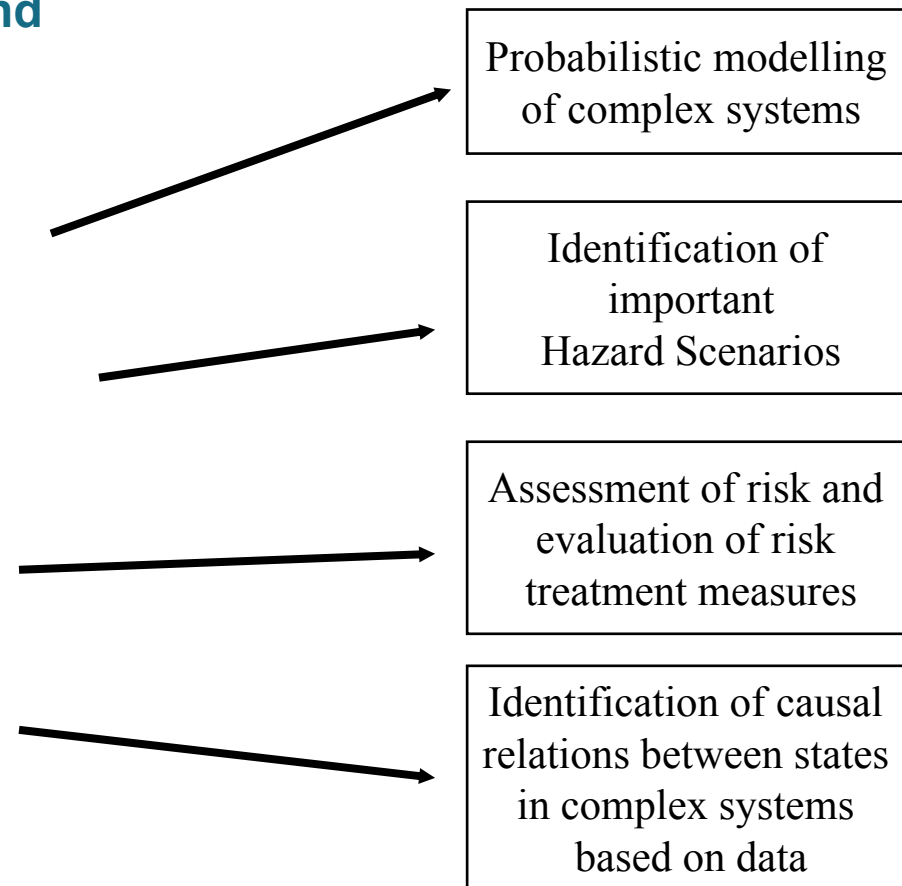
Possible to treat uncertainties consistently !

- Supporting the expert in decision making !
- Not replacing the expert !

# Introduction to Bayesian Probabilistic Nets (BPN's)

The theory of Bayesian Probabilistic Networks has developed rapidly and includes

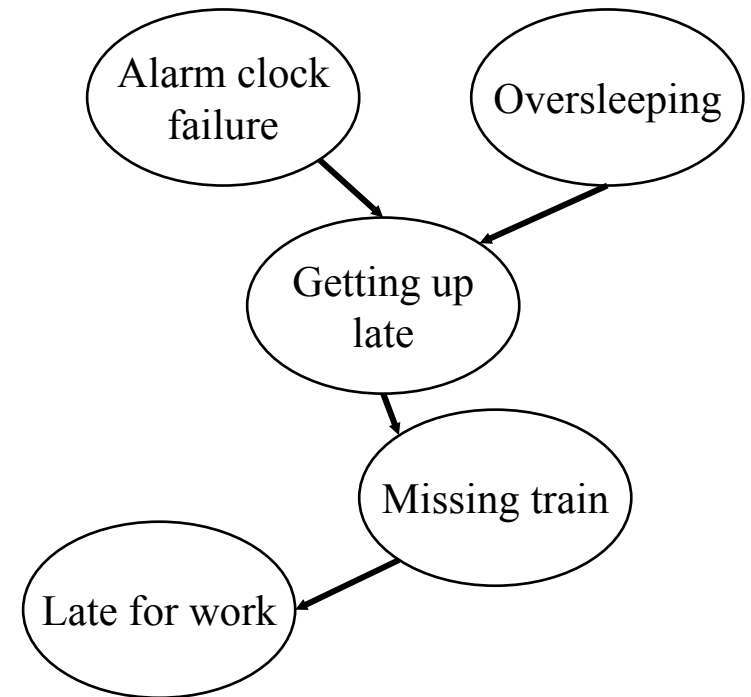
- Establishing multi-variate joint probability structures
- Diagnostics of technical systems and in medicine
- Decision analysis subject to uncertainty
- Inference and data mining



# Causality as a support in reasoning

## Causality and Reasoning

Causal networks are graphical representations of causally interrelated events



# Causality as a support in reasoning

## Causality and Reasoning

In our daily lives we reason on the basis of causal relations

Consider the following situation

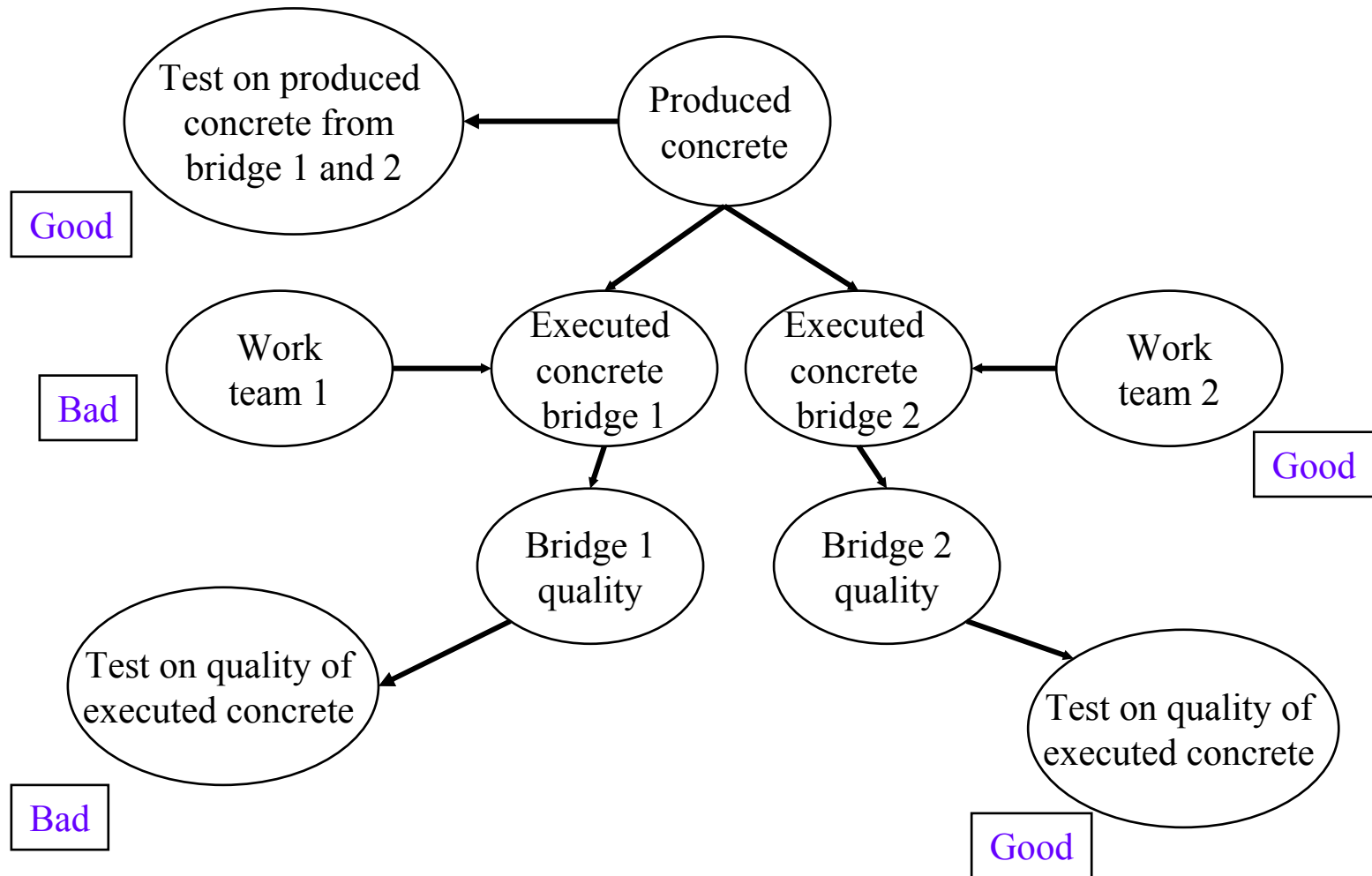
You are the owner of two new and almost identical bridges 1 and 2 made of concrete produced on site (small factory)

- tests performed on bridge 1 indicates that the quality of the executed concrete of bridge 1 is bad

The question is :

– What is the quality of the executed concrete of bridge 2?

# Causality as a support in reasoning



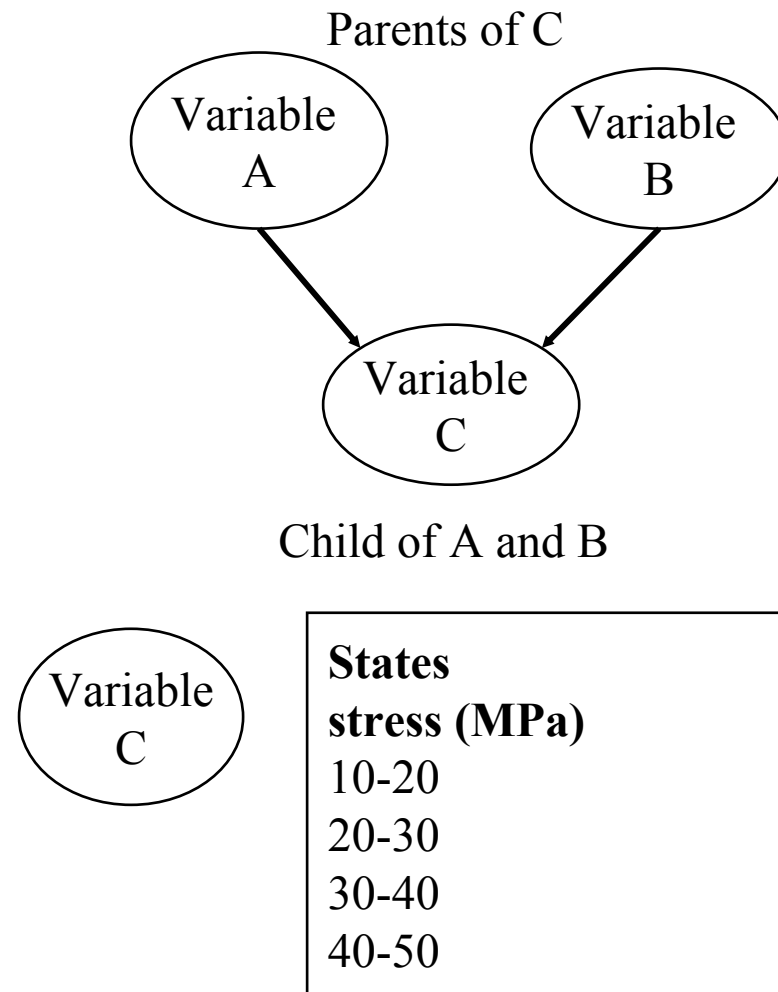


# Causality as a support in reasoning

## Causal and Bayesian Networks

Formally speaking :

- a directed graph representing the causal interrelation between uncertain events
- interrelations expressed in terms of “family relations”
- a variable can have any number of discrete states or a continuous state space

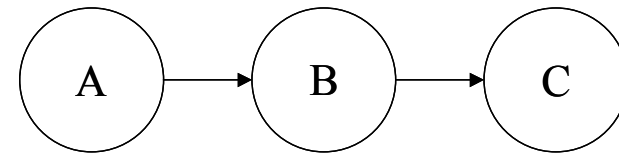


# Basic theory of BPN's with discrete states

Networks can be categorized in accordance with their configuration

For serially connected networks :

Information may be passed only if the states of the connecting variables are unknown



**Serially connected network**

B depends on A, C depends on B

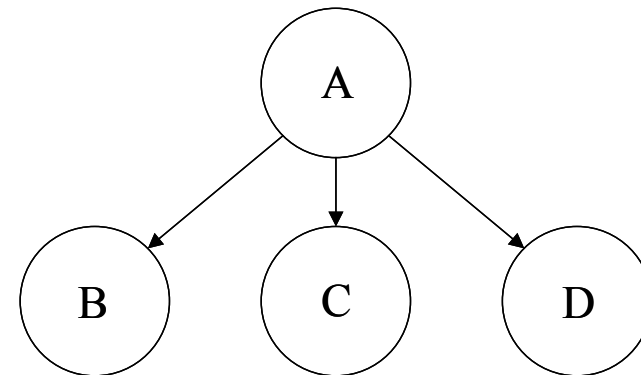
If the state of B is known with certainty variable A and variable B become independent

A and C are *d-connected* given B

# Basic theory of BPN's with discrete states

For diverging networks :

Information about any of the child variables will influence the uncertainty of the states of the other children as long as the state of the variable A is unknown



**Diverging network**

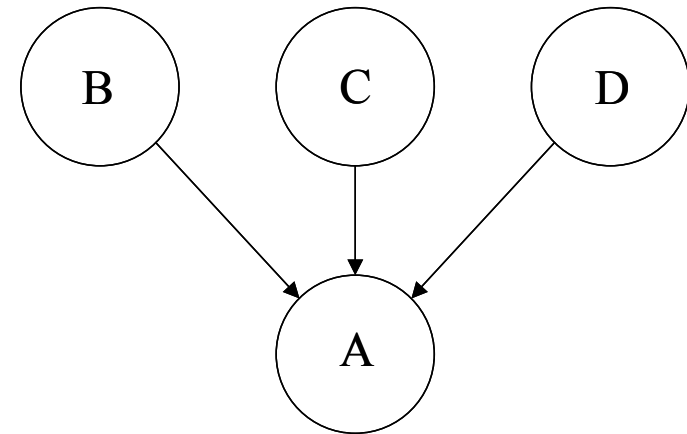
B, C and D depend on A

B, C and D are *d-connected* given A

# Basic theory of BPN's with discrete states

For converging networks :

Information about any of the child variables will influence the uncertainty of the states of the other children as long as the state of the variable A is unknown



**Converging network**

A depends on B, C and D

B, C and D are independent as long as the state of A is unknown

Given the state of A the variables B, C and D become dependent

# Basic theory of BPN's with discrete states

- Formally a Bayesian network is composed of:
  - A set of variables and a set of directed *edges* (or connections) between the variables.
  - Each variable may have a countable or uncountable set of mutually exclusive states.
  - The variables together with the directed edges form a directed a-cyclic graph (DAG)
  - To each variable  $A$  with parents  $B, C, D, ..$  there is assigned a conditional probability structure  $P(A|B,C,D,..)$

# Basic theory of BPN's with discrete states

Assume that all  $n$  variables  $A_i$ ,  $i = 1, 2, \dots, n$  of a Bayesian Network are collected in the vector  $A = (A_1, A_2, \dots, A_n)^T$  - also called the *universe*  $U$ .

In general it is of interest to be able to assess:  $P(\mathbf{U}) = P(A_1, A_2, \dots, A_n)$

the joint probability distribution of the universe i.e. ,

any marginalized set of the universe  $P(A_i)$  as well as to

assess such probability distributions subject to *evidence* in regard to the states of individual variables, e.g.  $P(A_i|e)$  .

# Basic theory of BPN's with discrete states

A Bayesian Network can be considered to be a special representation of such probability distributions and using the so-called chain rule of probability calculus it is possible to write the probability distribution function in the following form:

$$P(\mathbf{U}) = \prod_i P(A_i | pa(A_i))$$

where  $pa(A_i)$  is the parent set of the variable  $A_i$  .

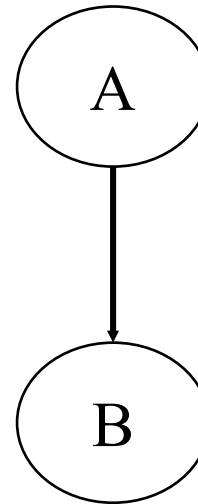
The probability distribution function for elements of  $\mathbf{U}$  , e.g. for  $A_j$

can be achieved by *marginalization* i.e.  $P(A_j) = \sum_{\mathbf{U} \setminus A_j} P(\mathbf{U}) = \sum_{\mathbf{U} \setminus A_j} \prod_i P(A_i | pa(A_i))$

# Basic theory of BPN's with discrete states

Bayesian networks are sometimes referred to as **directed acyclic graphs (DAG's)**

The states of each variable is allocated a conditional probability structure



State	Probability
<b>Wind speed</b>	
0-10 (m/s)	0.6
10-20 (m/s)	0.4

State	Probability	
<b>Wind force</b>	<b>Wind speed (m/s)</b>	
	<b>0-10</b>	<b>10-20</b>
50-60 (kN)	0.6	0.3
60-70 (kN)	0.4	0.7



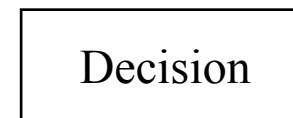
# Bayesian Probabilistic Networks

Bayesian Networks may in addition to uncertain variables include

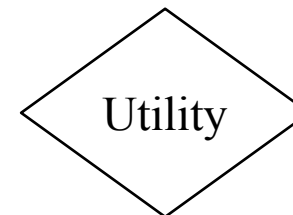
- decision nodes
- utility nodes

Decision nodes contain the various actions which may be decided

Utility nodes prescribe the consequences given the state of the variables and the decisions



Do nothing  
Modify system

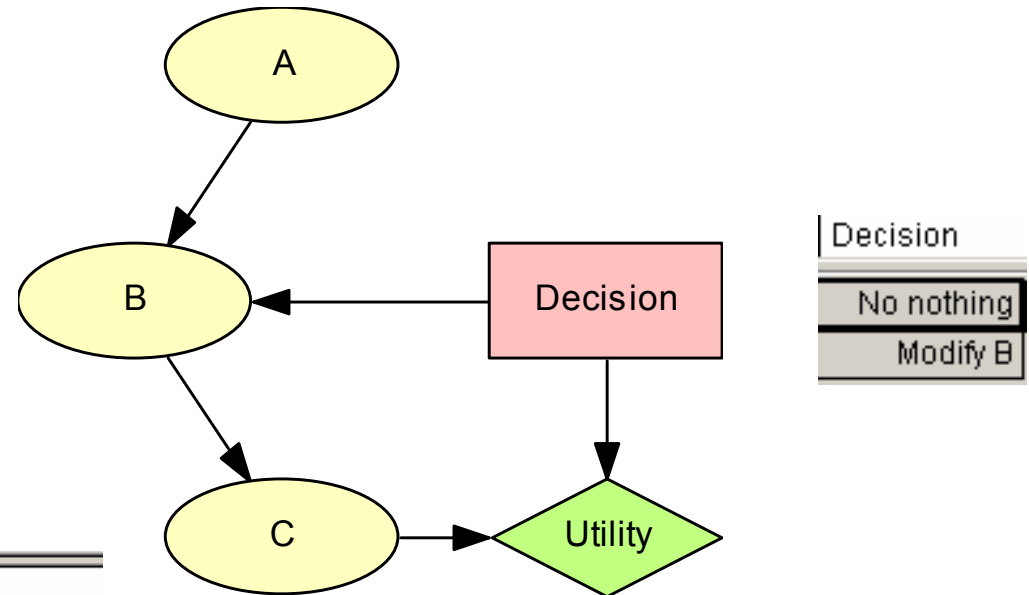


Consequences  
- costs  
- fatalities  
- injuries  
- environmental impact

# Bayesian Probabilistic Networks

The probabilities assigned to the states of a variable may be conditional on the decisions

The utility may be given as a function of the states of the variables and the decisions



B					
Decision		No nothing		Modify B	
A	fail	safe	fail	safe	
fail	0.5	0.2	0.3	0.05	
safe	0.5	0.8	0.7	0.95	

Utility					
Decision		No nothing		Modify B	
C	fail	safe	fail	safe	
Utility	1000	0	1001	1	

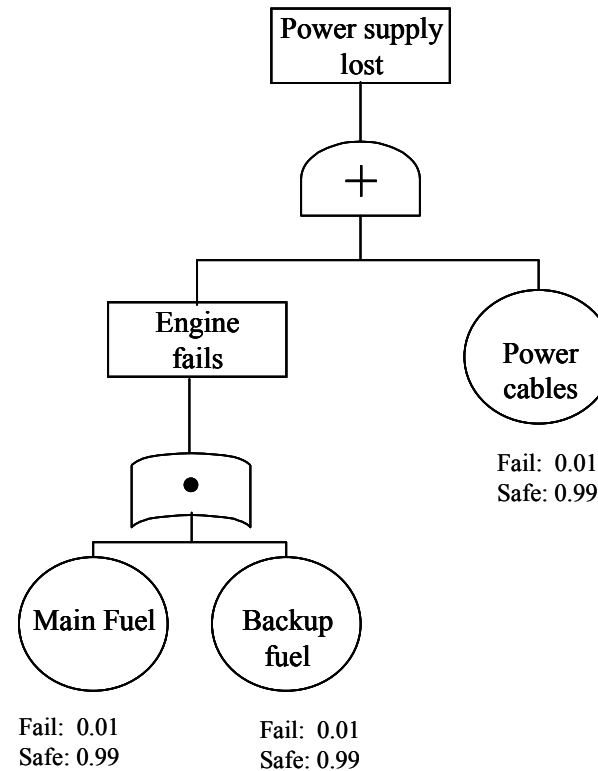
# Risk analysis and decision making using BPN's

## Bayesian Networks for Risk Analysis

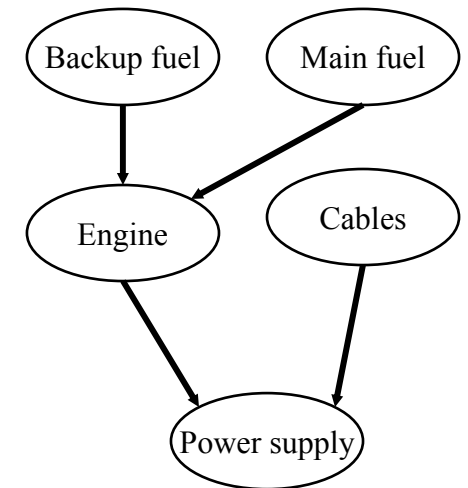
BPN's may readily substitute fault trees, event trees, cause consequence charts and decision trees in risk analysis

No problems with common cause failures when using PBN's.

Let us consider the simple power supply example again



Fault tree

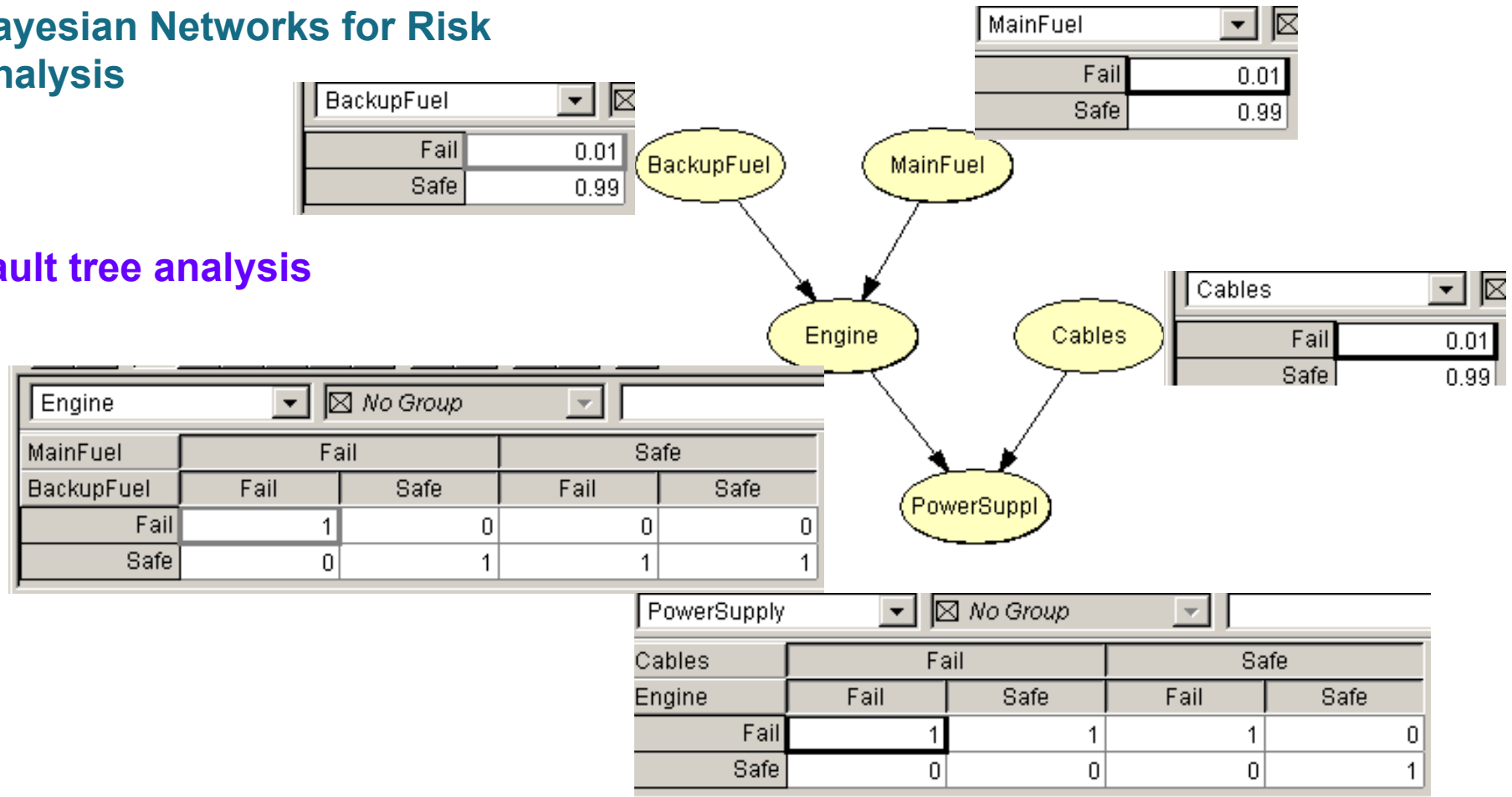


BPN

# Risk analysis and decision making using BPN's

## Bayesian Networks for Risk Analysis

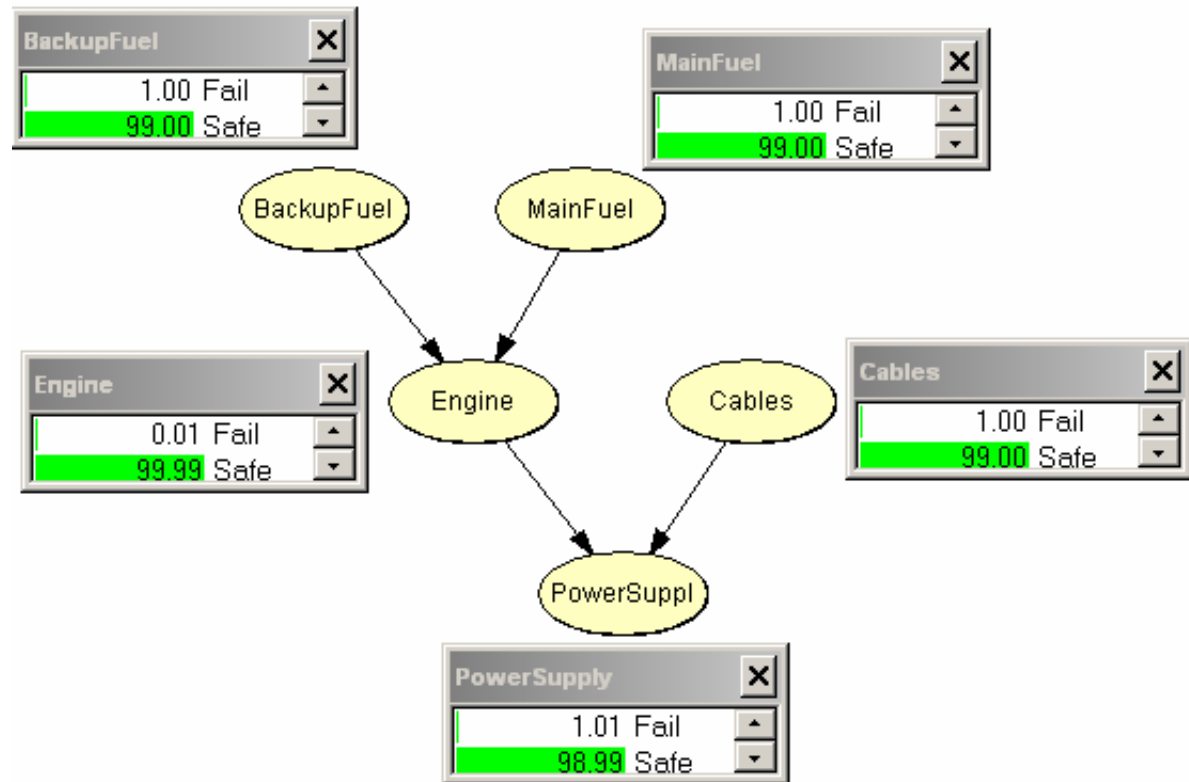
## Fault tree analysis



# Risk analysis and decision making using BPN's

Bayesian Networks for Risk Analysis

Fault tree analysis

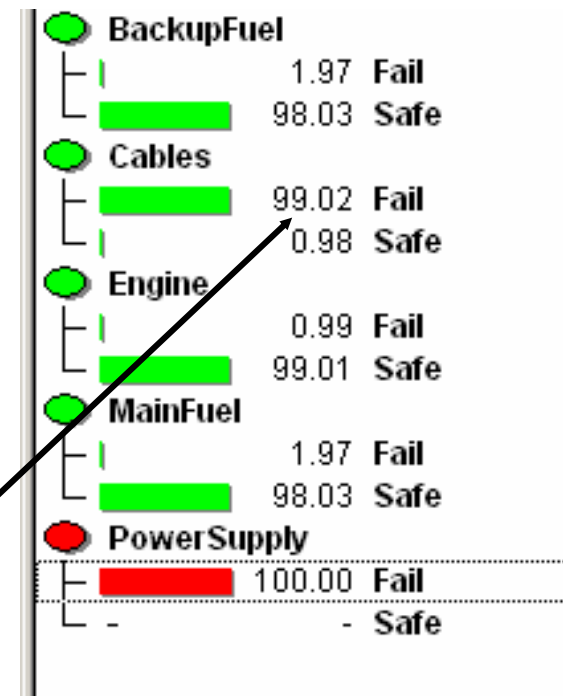


# Risk analysis and decision making using BPN's

Bayesian Networks for Risk Analysis

Identification of important hazard scenarios

Conditioning on the event of failure of power supply

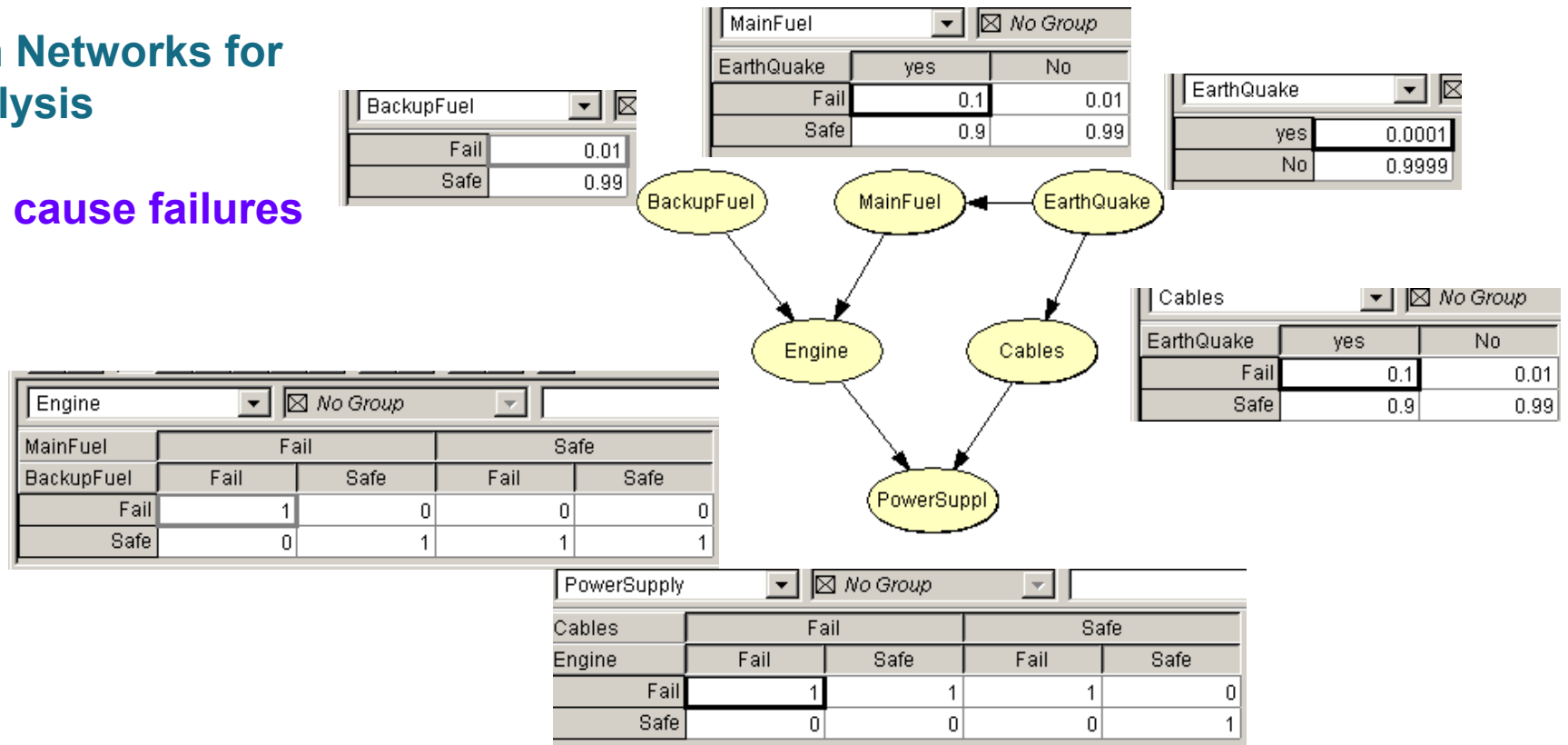


Most likely scenario is cable failure  
- this scenario should be detailed further in the modelling

# Risk analysis and decision making using BPN's

## Bayesian Networks for Risk Analysis

### Common cause failures

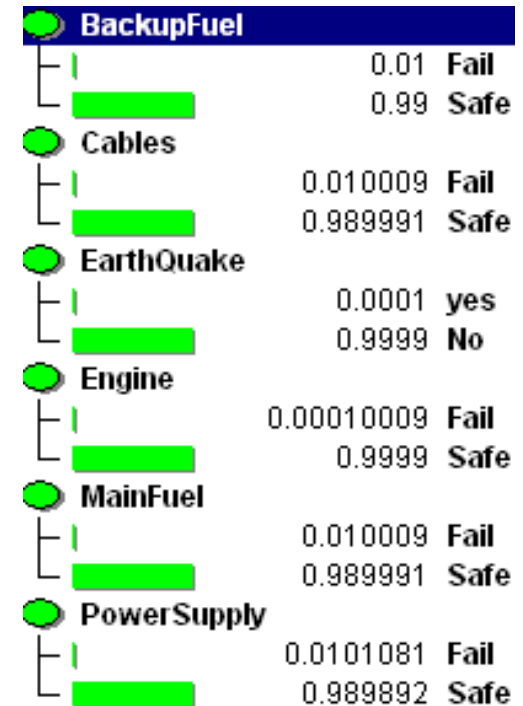


# Risk analysis and decision making using BPN's

## Bayesian Networks for Risk Analysis

### Common cause failures

With common cause	1.01081 %
Without common cause	1.00099 %

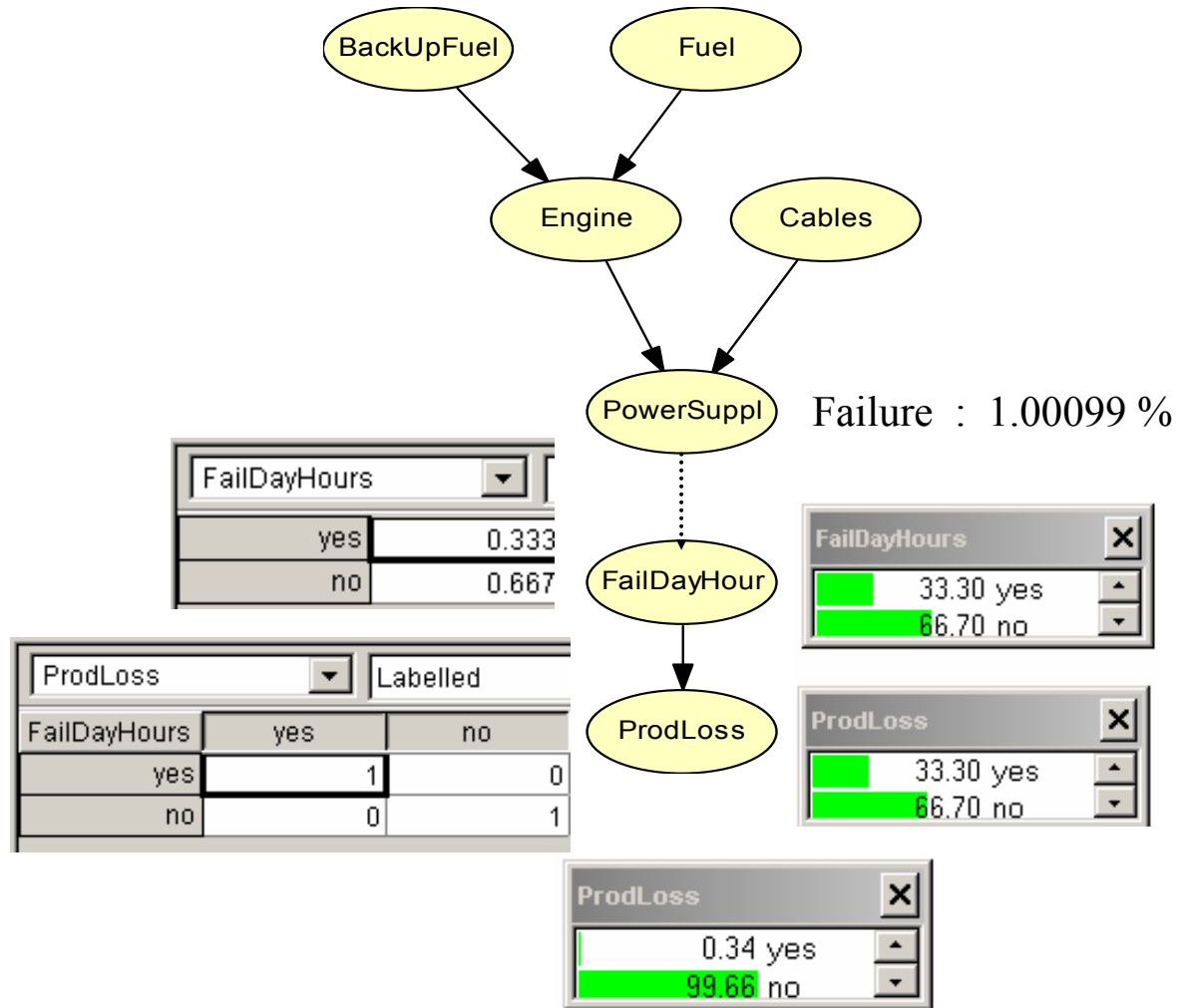




# Risk analysis and decision making using BPN's

## Bayesian Networks for Risk Analysis

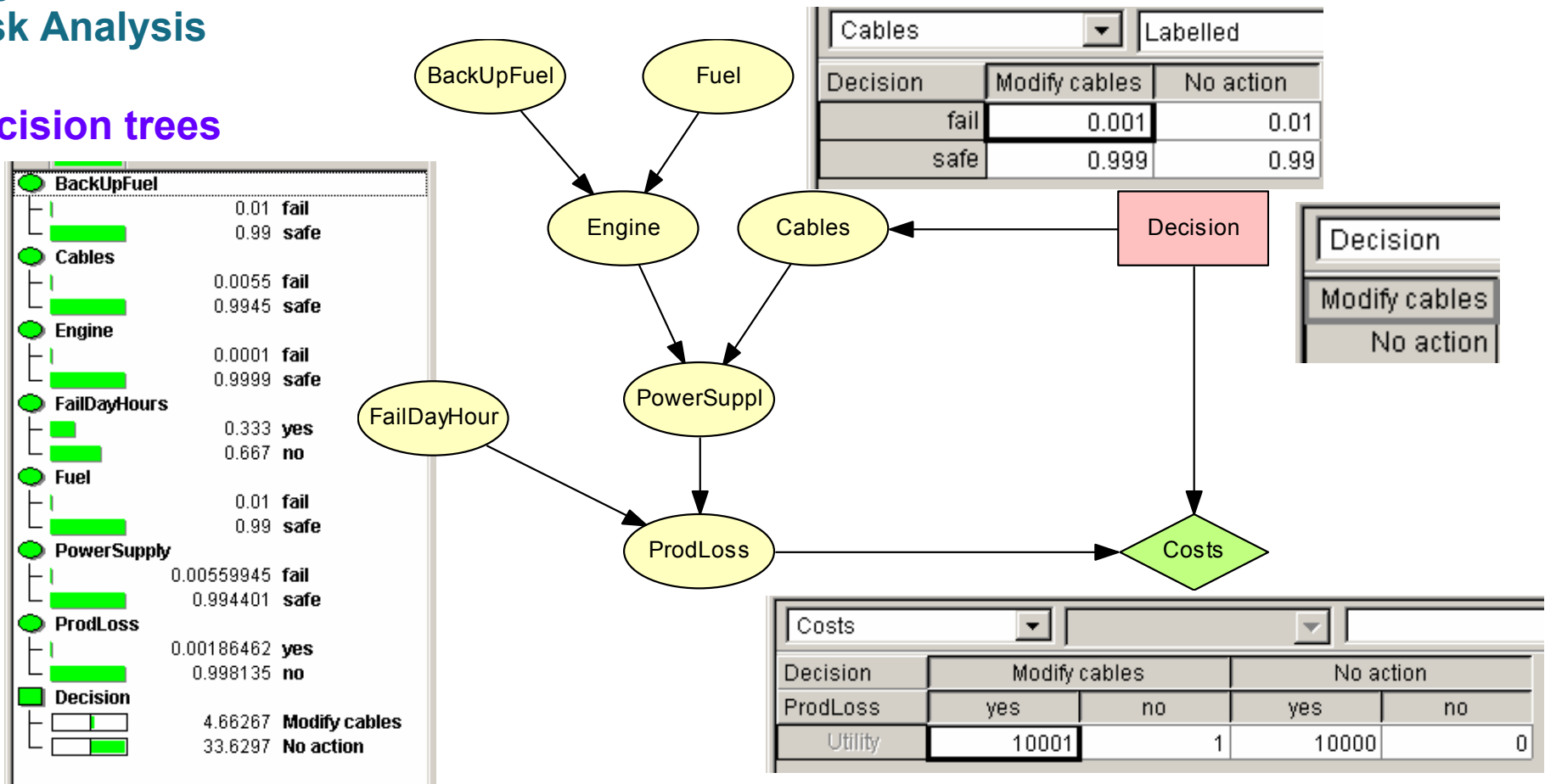
### Event trees



# Risk analysis and decision making using BPN's

## Bayesian Networks for Risk Analysis

### Decision trees



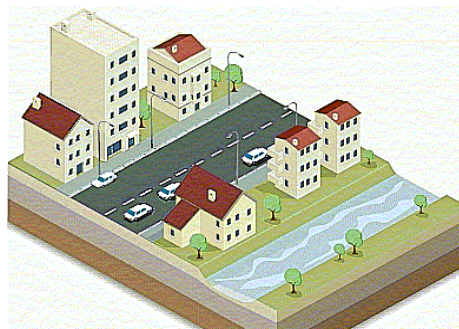
# Large Scale Risk Assessment using GIS and BPN's

- Risk management concerning natural hazards often involves large geographical areas



# Large Scale Risk Assessment using GIS and BPN's

- It is important to be able to provide decision support in the situations before, during and after the event of natural hazards

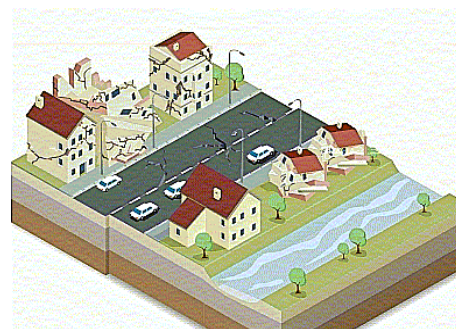


**Before**

Optimal allocation of available resources for risk reduction

- strengthening
- rebuilding

in regard to possible earthquakes

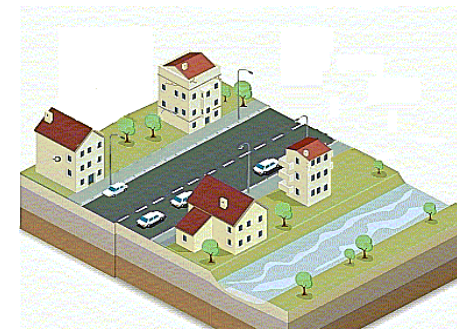


**During**

Damage reduction/Control

Emergency help and rescue

After quake hazards



**After**

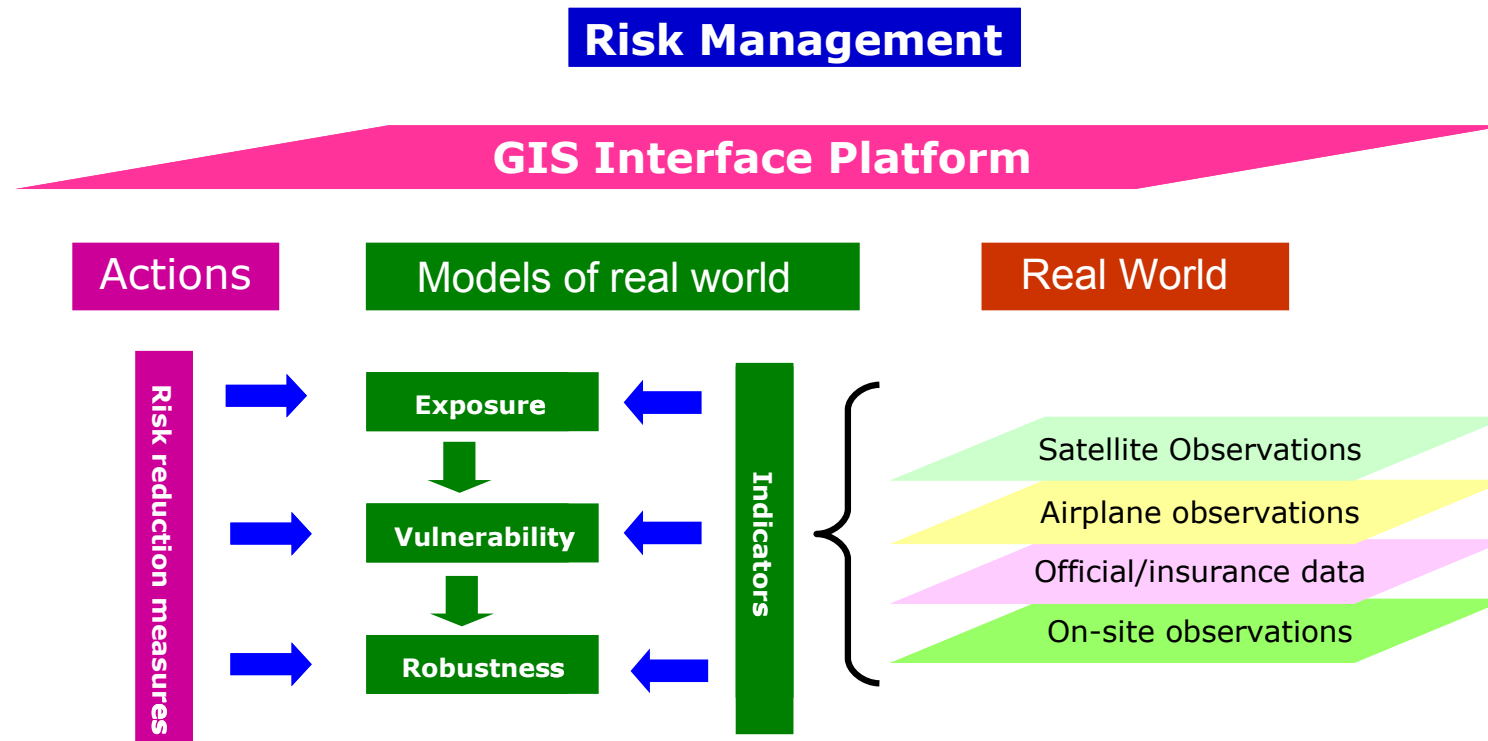
Rehabilitation of infrastructure functionality

Condition assessment and updating of reliability and risks

Optimal allocation of resources for rebuilding and strengthening

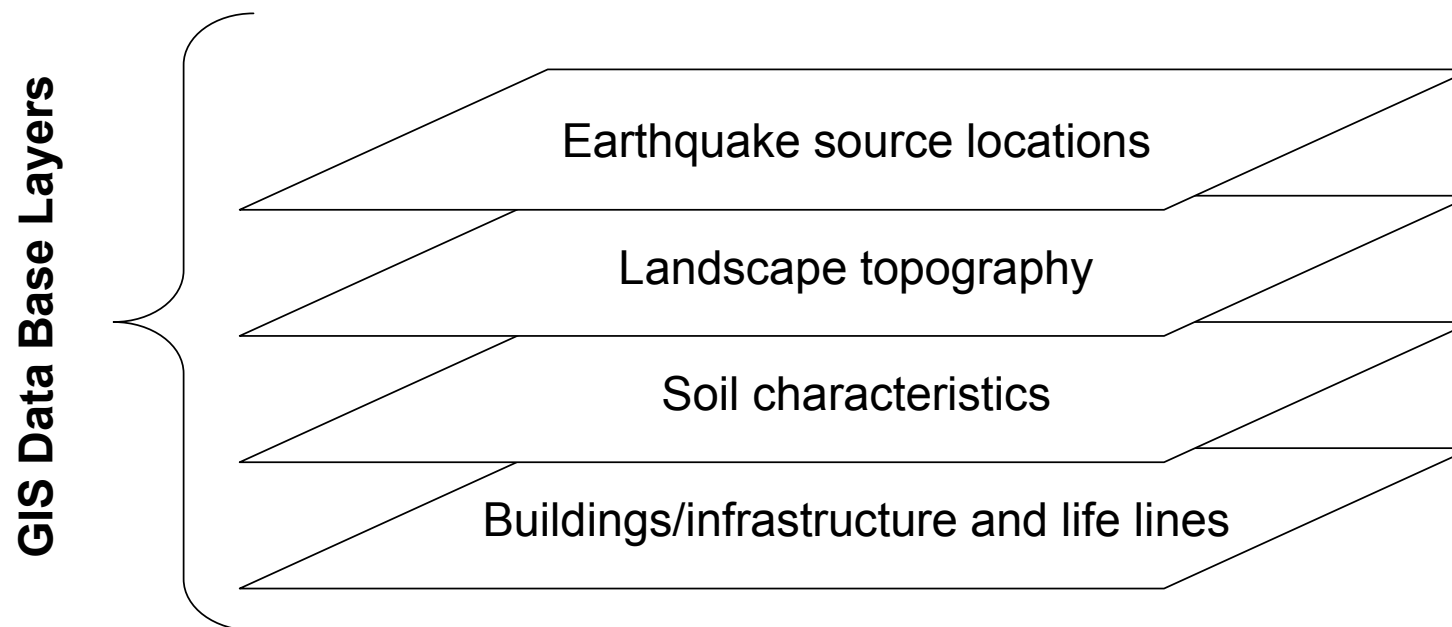
# Large Scale Risk Assessment using GIS and BPN's

- A general framework for natural hazards risk management using GIS can be visualized as:



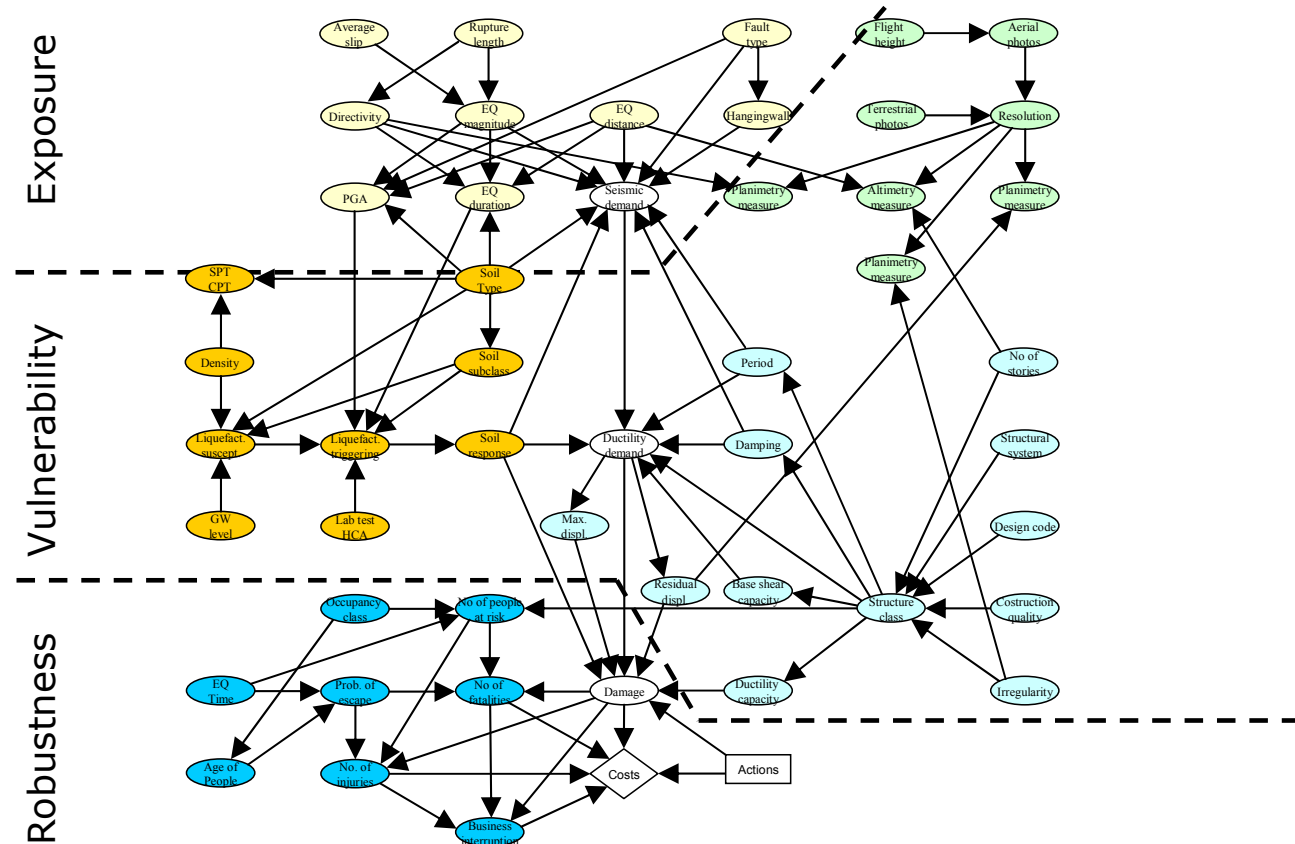
## Large Scale Risk Assessment using GIS and BPN's

- The GIS database is important as the many required data generally are spatially distributed for the considered system, e.g. city or region



# Large Scale Risk Assessment using GIS and BPN's

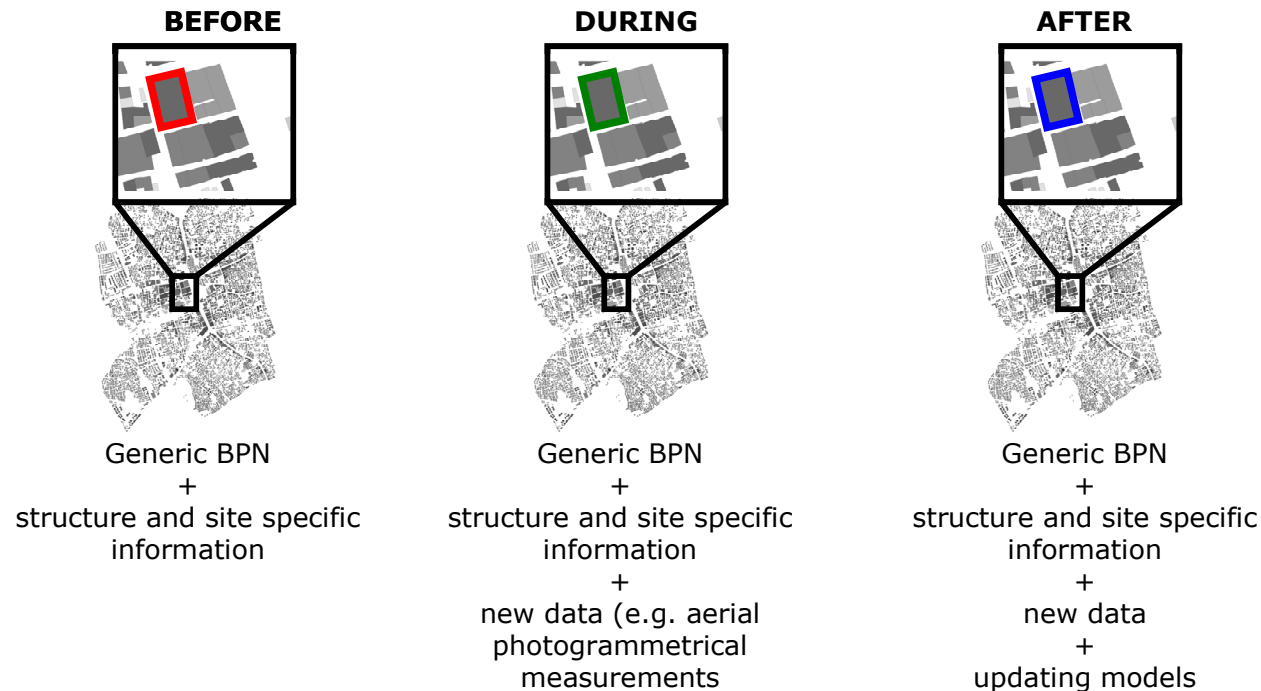
- Utilizing that indicators of exposures (hazards), and consequences (vulnerability and robustness) can efficiently be stored and managed in the GIS data base, BPN risk models may be established and linked to each asset in the considered system



# Large Scale Risk Assessment using GIS and BPN's

- Utilizing that indicators of exposures (hazards), and consequences (vulnerability and robustness) can efficiently be stored and managed in the GIS data base, BPN risk models may be established and linked to each asset in the considered system

## Typical Outputs





# Large Scale Risk Assessment using GIS and BPN's

- The generic BPN risk models linked with the GIS database facilitate the efficient risk assessment for large numbers of buildings and other assets



## Damage State

- Fully Operational
- Operational
- Life Safety
- Near Collapse
- Collapse

# Large Scale Risk Assessment using GIS and BPN's

- The generic BPN risk models linked with the GIS database facilitate the efficient risk assessment for large numbers of buildings and other assets

