

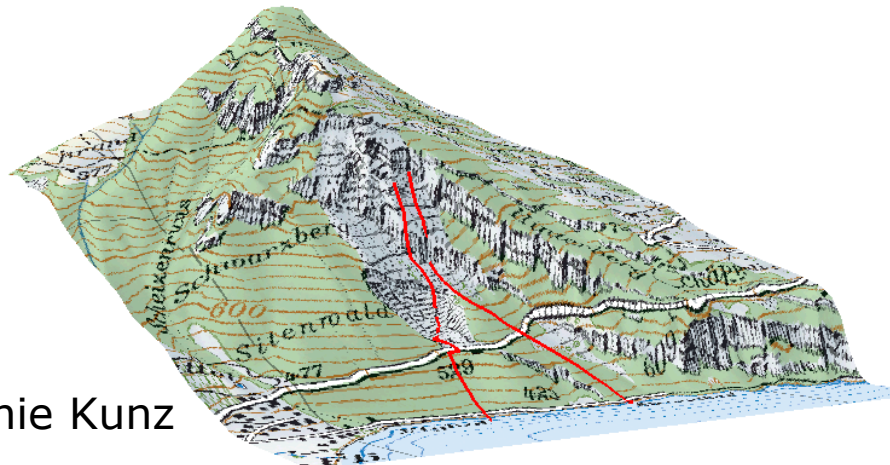
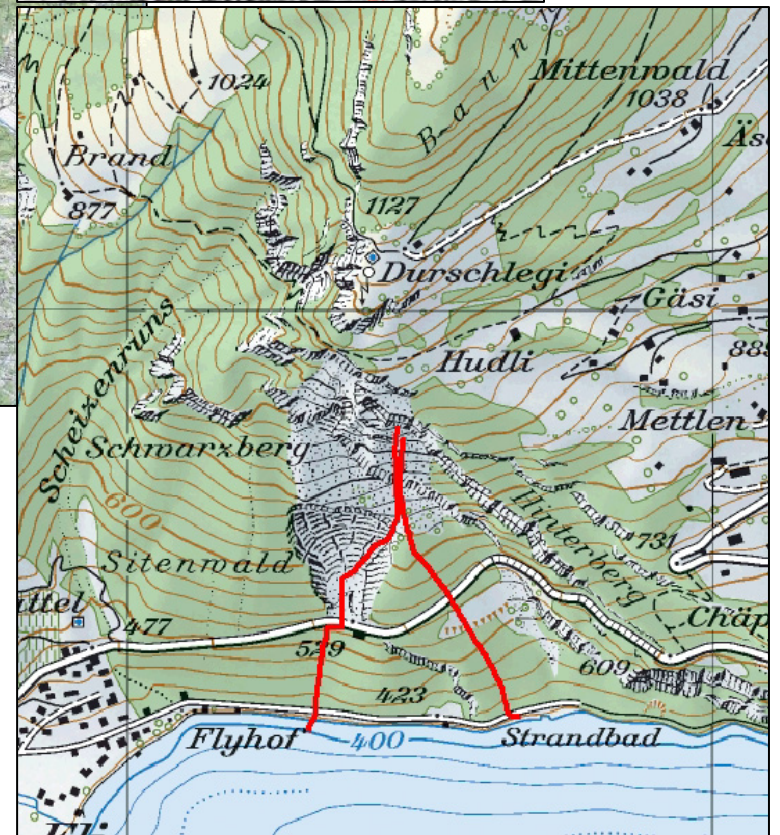
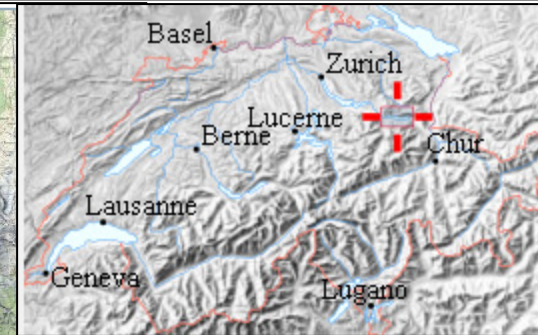
Rockfall study

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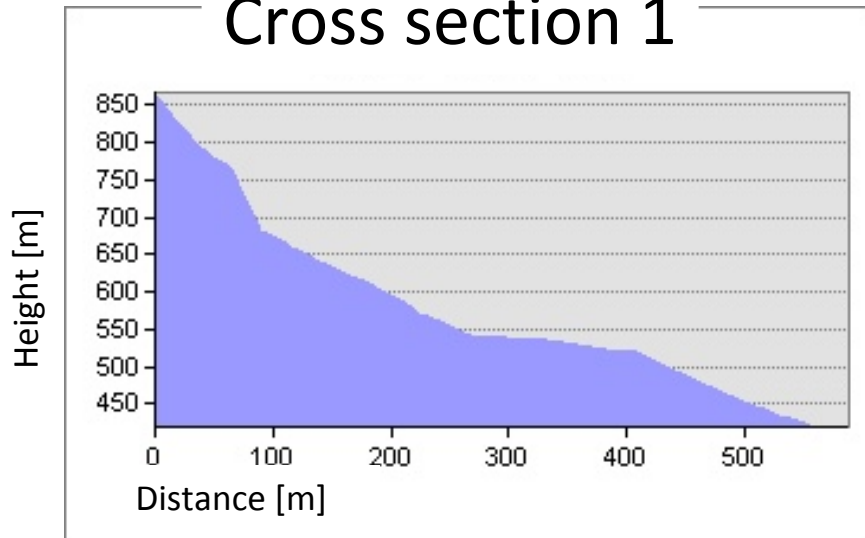
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 - Two slopes
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Test site: Durschlegli area near Weesen, SG

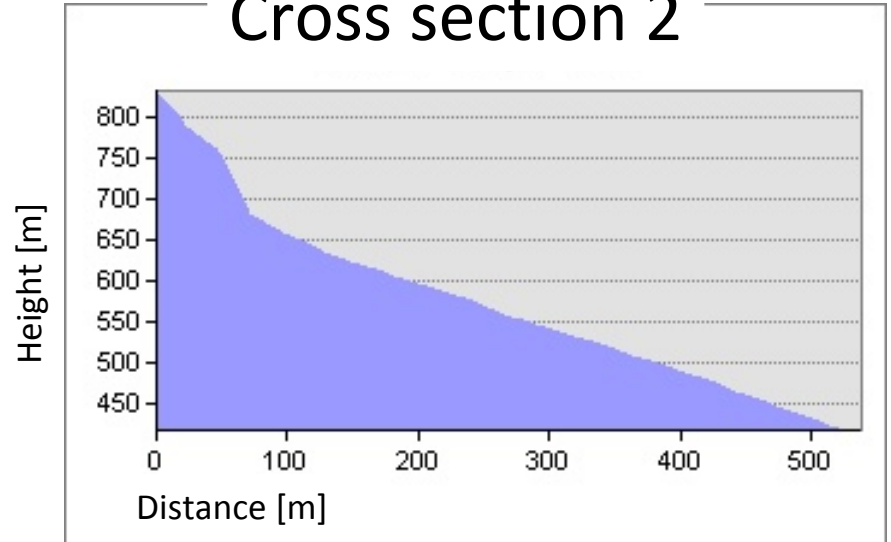


Test site: Durschlegli area near Weesen, SG

Cross section 1



Cross section 2



Use and indicators for hazard maps

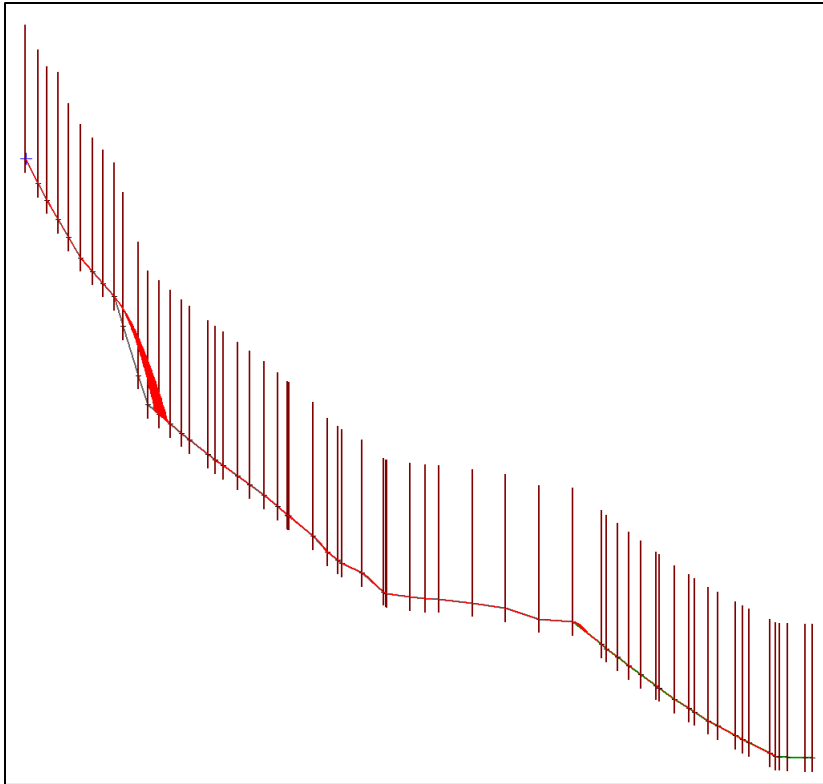
Use of hazard map	Inclusion of existing protection measures	Human safety and/or economic loss	Indicators (energy, velocity or volume, etc.)	Way of representation (exceedance probability or physical value)
Warning to hikers	Yes	Human safety	Any rockfall	Exceedance probability
Planning/installation/maintenance of protection measures	No	Both	Energy	Physical value
Land use planning	Depending	Both	Energy	Physical value

Computation of the rock fall trajectories

- Using the program RocFall (Rocscience)
- One rock counter in each slope definition point
- Slope material:
 - Helveticum in the upper part & detachment zone
 - Coefficients of restitution:
 - Tangential $\mu = 0.615$; $\sigma = 0.092$
 - Normal $\mu = 0.303$; $\sigma = 0.045$
 - Vegetated soil in the lower part
 - Coefficients of restitution:
 - Tangential $\mu = 0.800$; $\sigma = 0.040$
 - Normal $\mu = 0.300$; $\sigma = 0.040$
- Point source on top of the slope, 10,000 runs
- Outcome: Rock fall count and velocity distribution
- Independent of stones volume/mass

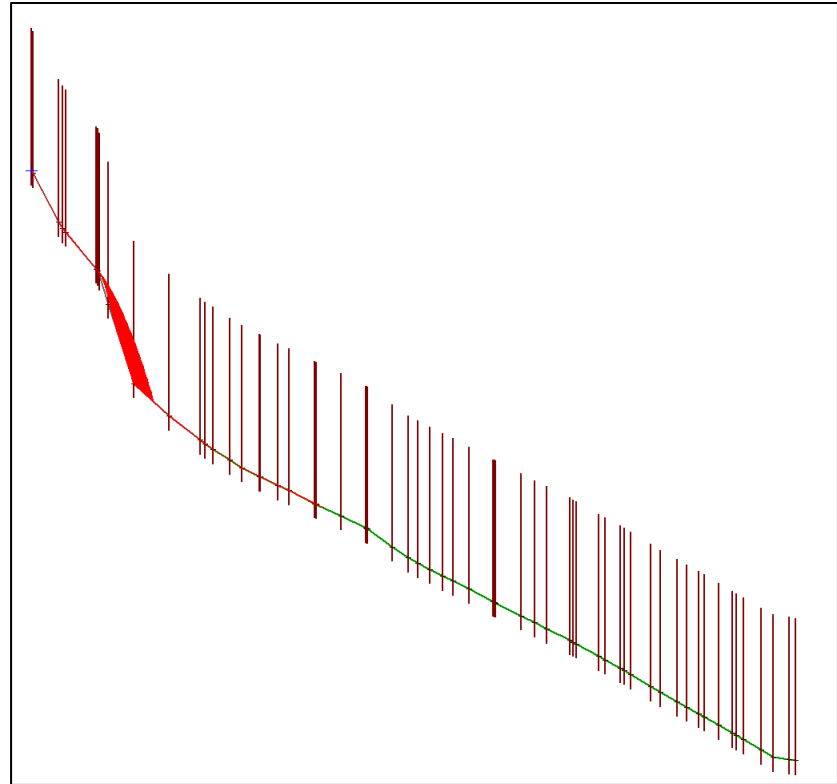
Computation of the rock fall trajectories

Cross section 1



584 rocks reach the bottom of the slope

Cross section 2



Rocks stop in the vegetated zone

Detachment model

- The exceedance frequency can be described by , e.g.:

$$H_V(v|\theta) = a v^{-b}$$

- Include the epistemic uncertainties by modeling the parameters (A,B) as a random vector $\theta = [a,b]^T$

$$f_{\Theta}(\theta) \quad \Theta \sim LN(\mu_{a'}, \mu_{b'}, \sigma_{a'}, \sigma_{b'}, \rho_{a,b})$$

- The unconditional exceedance frequency can be calculated:

$$H_V(v) = \int_{\Theta} H_V(v|\theta) f_{\Theta}(\theta) d\theta$$

- Derivation of the annual maximum rockfall event distribution function $f_V(v)$ from the exceedance frequency $H_V(v)$:

$$f_V(v) = \frac{d}{dv} (\exp(-H_V(v)))$$

Detachment model

- Estimation of exceedance frequency for volume classes by the 2.5% and 97.5% fractile
 - Constant mean of frequency
 - Coefficients of variation: 0.1 and 1.0

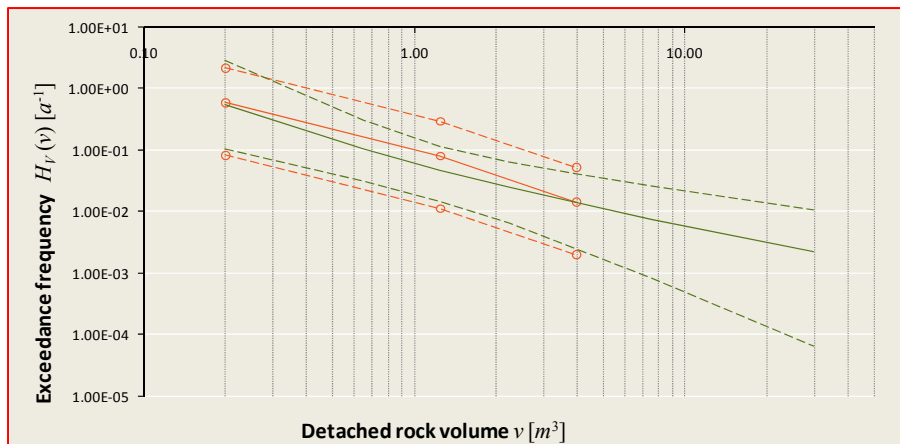
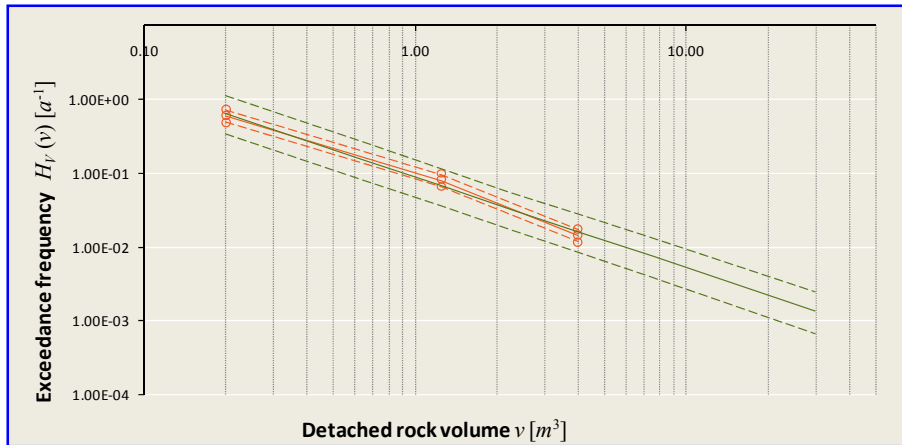
Range [m^3]	Rep. Value [m^3]	Exceedance Frequency $H_X(x_i) [a^{-1}]$				μ	
		$Q_{0.025} [a^{-1}]$		$Q_{97.5} [a^{-1}]$			
		CoV 0.1	CoV 1.0	CoV 0.1	CoV 1.0		
0.1	0.3	0.20	$4.91 \cdot 10^{-1}$	$7.259 \cdot 10^{-1}$	$8.297 \cdot 10^{-2}$	$2.169 \cdot 10^0$	$6.00 \cdot 10^{-1}$
0.3	1.0	0.65	N/A	N/A	N/A	N/A	N/A
1.0	1.5	1.25	$6.649 \cdot 10^{-2}$	$9.830 \cdot 10^{-2}$	$1.123 \cdot 10^{-2}$	$2.937 \cdot 10^{-1}$	$8.125 \cdot 10^{-2}$
1.5	3.0	2.25	N/A	N/A	N/A	N/A	N/A
3.0	5.0	4.00	$1.175 \cdot 10^{-2}$	$1.737 \cdot 10^{-2}$	$1.986 \cdot 10^{-3}$	$5.192 \cdot 10^{-2}$	$1.436 \cdot 10^{-2}$
5.0	10	7.50	N/A	N/A	N/A	N/A	N/A
10	50	30.0	N/A	N/A	N/A	N/A	N/A

- Parameter estimation by method of maximum likelihood

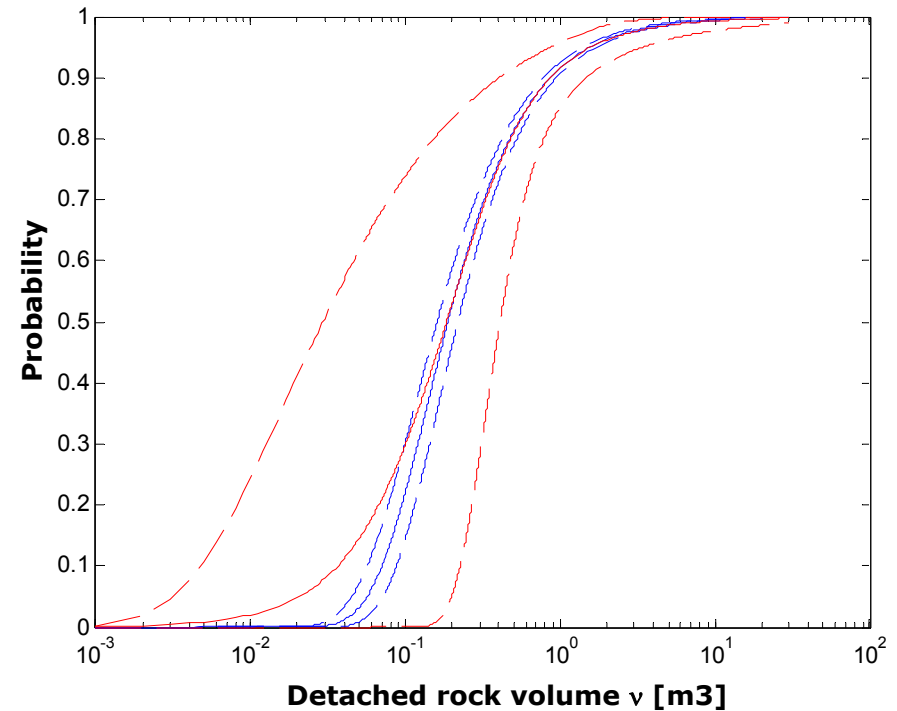
	μ_a	μ_b	σ_a	σ_b	ρ_{ab}
CoV 0.1	$8.835 \cdot 10^{-2}$	$1.232 \cdot 10^0$	$5.089 \cdot 10^{-3}$	$4.671 \cdot 10^{-2}$	$4.849 \cdot 10^{-5}$
CoV 1.0	$6.280 \cdot 10^{-2}$	$1.232 \cdot 10^0$	$3.010 \cdot 10^{-2}$	$3.906 \cdot 10^{-1}$	$-3.383 \cdot 10^{-3}$

Detachment model

Exceedance frequency
CoV=0.1 and CoV=1.0



CDF for annual maximum
rockfall event



Calculation of annual maximum energy

$$\text{Annual Maximum Energy} = 0.5 * \text{Rock density} * \text{Annual Maximum Detachment Volume} * (\text{Velocity})^2$$

Annual maximum detachment volume

- Calculated for the 2 sets of values/parameters for the detachment model (CoV=0.1 and CoV=10).
- A CDF curve is first randomly selected from the detachment model.
- A random probability value is then generated and the corresponding annual maximum detachment value is obtained.

Calculation of annual maximum energy

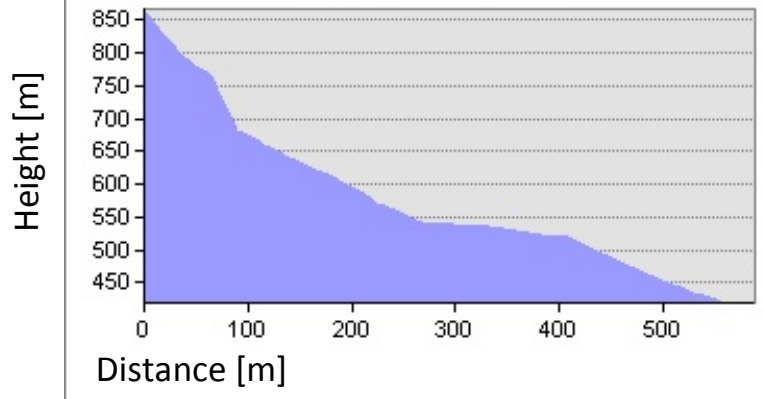
$$\text{Annual Maximum Energy} = 0.5 * \text{Rock density} * \text{Annual Maximum Detachment Volume} * (\text{Velocity})^2$$

Velocity

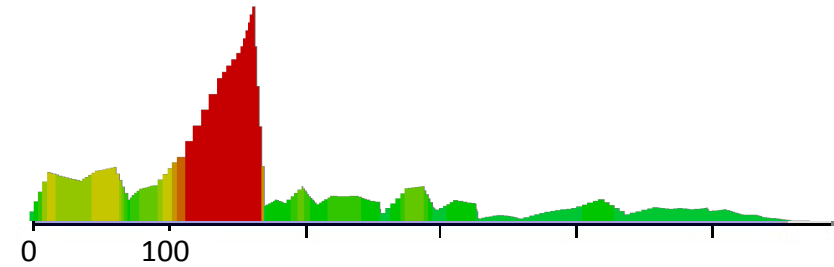
- A CDF is generated using the velocities obtained from the Roc-Fall program.
- A random probability value is then generated and the corresponding velocity is obtained.

Graphical representation of annual maximum energy

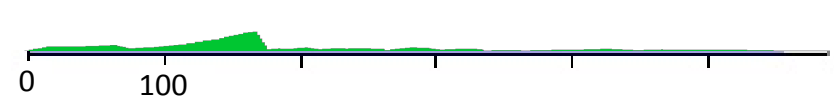
Cross section 1



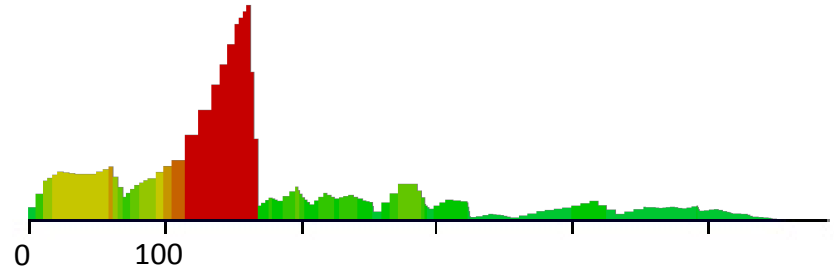
98% Quantile; Detachment CoV=0.1



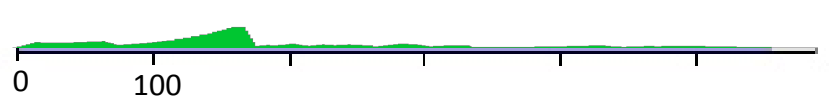
50% Quantile; Detachment CoV=0.1



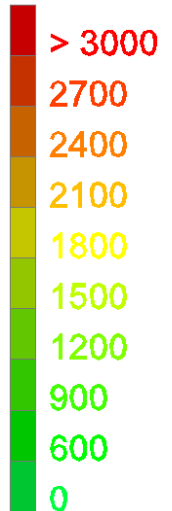
98% Quantile; Detachment CoV=1.0



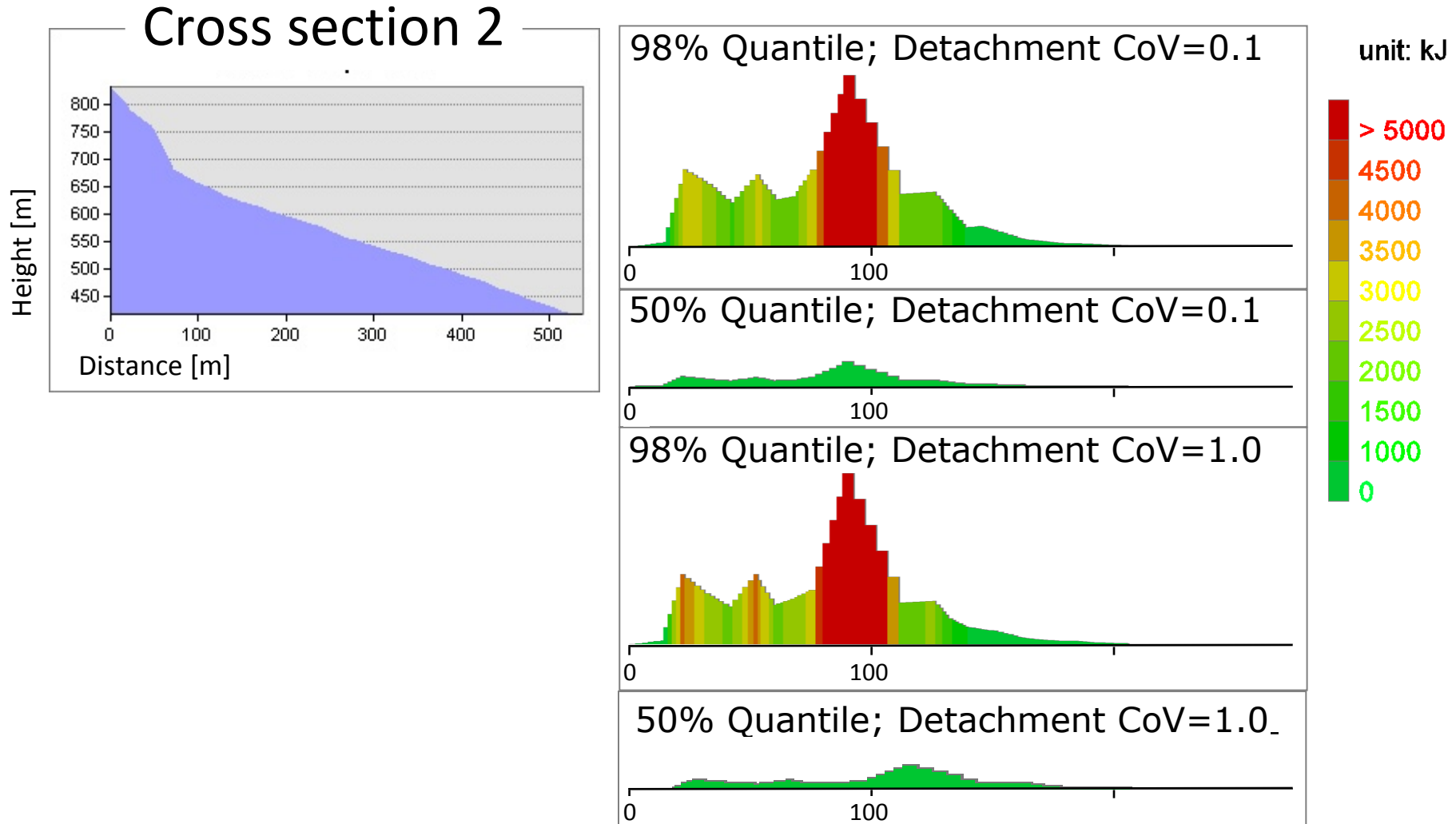
50% Quantile; Detachment CoV=1.0



unit: kJ

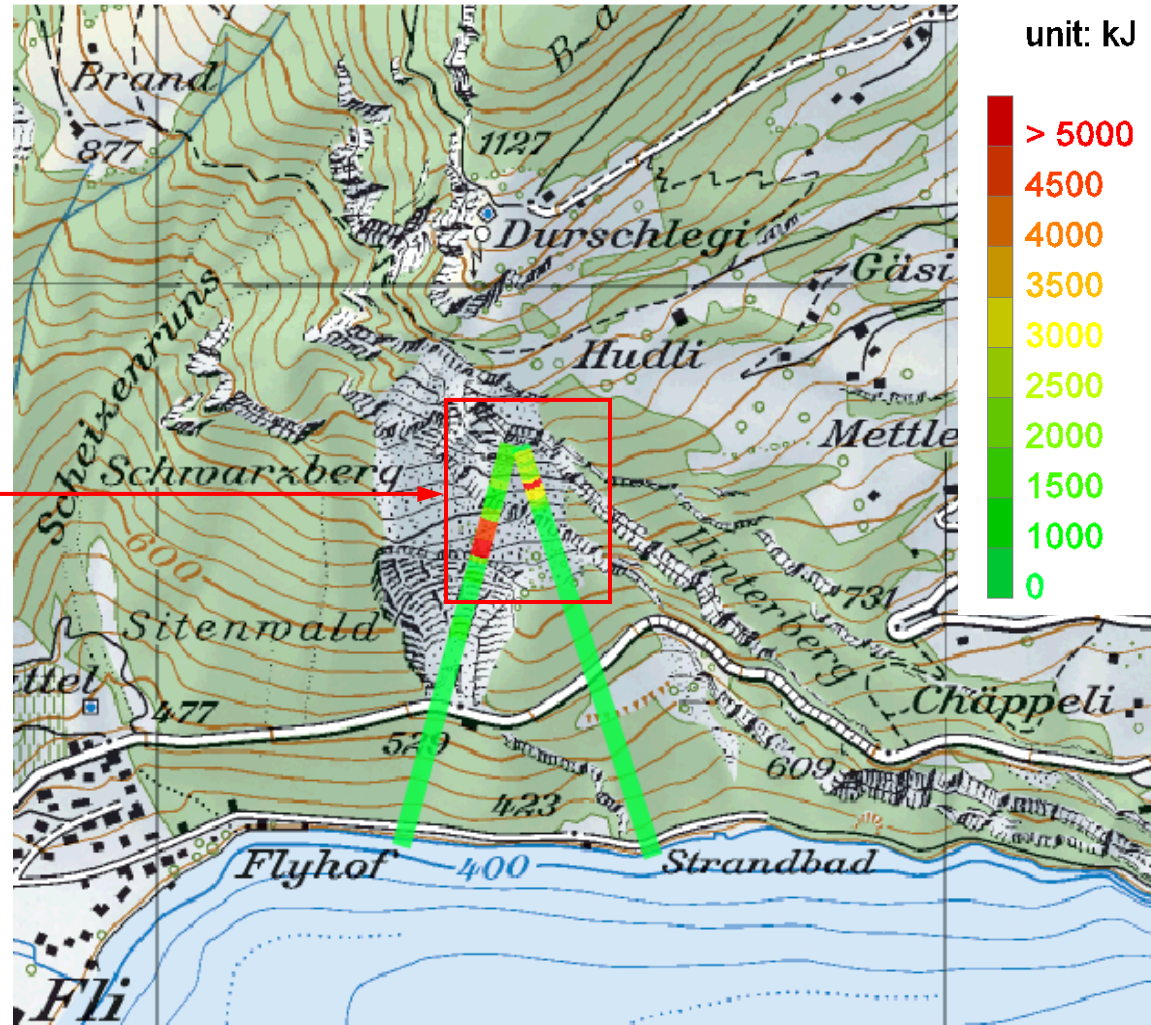
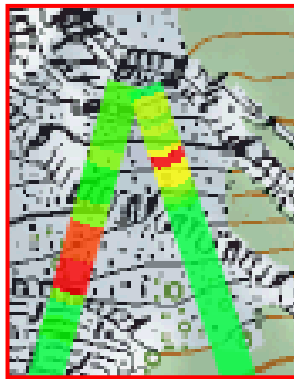


Graphical representation of annual maximum energy



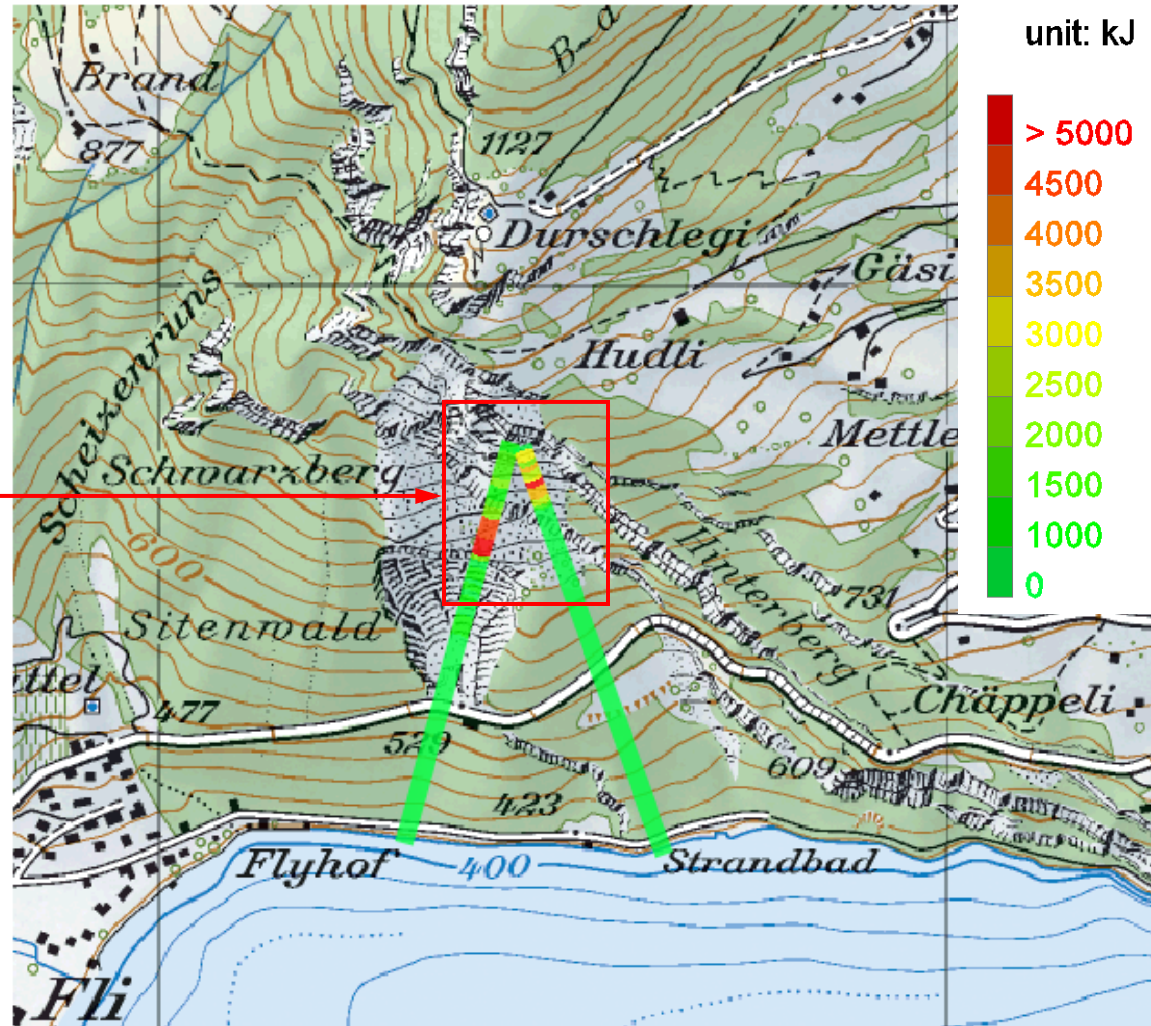
Graphical representation of annual maximum energy

- Hazard map for both slopes with Detachment $CoV=0.1$ using the 98% quantile



Graphical representation of annual maximum energy

- Hazard map for both slopes with Detachment $CoV=1.0$ using the 98% quantile



Comments

- Combination of trajectory model and detachment model

$$f_V(v) = \frac{d}{dv} \left(\exp(-H_V(v)) \cdot h_T \right)$$

- Relative frequency of stones reaching a certain point on the slope: h_T
 - Assumption: The distribution function of the exceedance frequency per volume H_V does not change
- This combination was not considered
 - Only a small part of the slope is affected by the relative frequency of stones
 - For further refinement the trajectory model should include dependency on the volume of the stones

Summary

- Rockfall
 - Bottom of the slope 1 is reached for a small number of rocks
 - Slope 2: Rocks stop in the vegetated zone
- Detachment model
 - Geologist estimations and epistemic uncertainties have great influence on the detachment model
- Hazard map
 - Enlarging uncertainties of detachment frequency estimation enlarges quantile energies
 - Distribution of maximum annual energy along the slope is only minor influenced by different uncertainties in the detachment model